NTSE STAGE - I (DELHI STATE) 05 - A (2019 - 20) (For Class - X) MENTAL ABILITY TEST (MAT) HINTS & SOLUTIONS

1.
2
Positive factors of 256 are
1, 2, 4, 8, 16, 32, 64, 128, 256
$$\therefore sq = \frac{a(r^n - 1)}{(r - 1)} = \frac{1(2^9 - 1)}{(2 - 1)} [where a = 1, and r = 2, and n = 9]$$

$$\therefore Sq = 511$$

2.
$$\frac{X}{X+1} + \frac{X+1}{X} - \frac{1}{X(X+1)} = \frac{X^2 + (X+1)^2 - 1}{X(X+1)}$$
$$= \frac{X^2 + X^2 + 1 + 2X - 1}{X(X+1)} = \frac{2X^2 + 2X}{X(X+1)} = \frac{2X(X+1)}{X(X+1)}$$
$$= 2$$

3.
$$5+6+7+...+19$$

Here $a = 5$, $d = 1$ and $n = 15$

$$\therefore S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{15} = \frac{15}{2} (10+14\times1) = \frac{15}{2} \times 24$$

$$= 15 \times 12 = 180$$

4.
$$\frac{1}{2}:\frac{2}{3}:\frac{3}{4}=6:8:9$$

Let numbers be 6x, 8x and 9x

$$\therefore 9x - 6x = 27$$

.: Numbers are 54, 72, 81

5.
$$3^{25} + 3^{26} + 3^{27} + 3^{28} = 3^{25} (3^{0} + 3^{1} + 3^{2} + 3^{3})$$
$$= 3^{25} (1 + 3 + 9 + 27)$$
$$= 3^{25} \times 40 = 3^{23} \times 9 \times 5 \times 8$$
$$= 3^{25} \times 40 = 3^{23} \times 8 \times 45$$

6. Rohan's final score =
$$\frac{90 \times 2 + 75 \times 1}{3}$$
$$= 85$$

- 7.
- 7. Let Grand mother = G, mother = M and daughter = D
 ∴ Possible ways = GMD
 - GDM
 - MGD
 - MDG
 - DGM
 - DMG
- 8. 2
- 8. Let at time of marriage man's age = x years
 - And man's wife's age = y years

$$x = y + 6 ...(1)$$

And
$$(x+12) = \frac{6}{5}(y+12)$$

$$= 5x + 60 = 6y + 72$$

$$= 5x - 6y = 12...(2)$$

Solving both equations we got x = 24 and y = 18

- 9. 3
- 9. P (number is even) = $\frac{1}{2}$
 - P (number is less than 4) = $\frac{1}{2}$
 - P (number is even and less than 4) = $\frac{1}{6}$

$$\therefore P\left(\frac{\text{number is less than 4}}{\text{number is even}}\right) = \frac{P(\text{number is even and less than 4})}{P(\text{number is even})} = \frac{\frac{1}{6}}{\frac{1}{2}} = \frac{1}{3}$$

- 10. 2
- 10. 10 balls \rightarrow 5B and 5W

After removing 1 B balls, total balls left = 9 and

Total black balls left = 4

∴ P (B ball after removing 1st B ball) =
$$\frac{4}{9}$$

- 11. 2
- 11. $10-3=12 \rightarrow 10-3+5=12$

$$12 - 4 = 13 \rightarrow 12 - 4 + 5 = 13$$

$$14 - 5 = 14 \rightarrow 14 - 5 + 5 = 14$$

$$16 - 6 = ? \rightarrow 16 - 6 + 5 = 15$$

- 12. 2
- 12. If bus does not stops, then it will travel 9 km more with 54 kmph

$$\therefore \text{ It will stop for } \frac{9}{54} \text{hr} = \frac{9}{54} \times 60 \text{ min}$$

= 10 min

13.
$$\frac{40 \times 1620}{100} + \frac{30 \times 960}{100} = \frac{x \times 5200}{100}$$
$$\therefore x = \frac{40 \times 1620 + 30 \times 960}{5200}$$

14. Between 1st and 25th tree there are 24 gap & let say each gap is of x m distance.

$$\therefore 24 x = 30$$
$$x = \frac{30}{24}$$

Now between 3rd & 15th tree there are 12 gaps

$$\therefore$$
 Distance between 3rd & 15th tree = 12 $\times \frac{30}{24}$ = 15 m

16.
$$\frac{80A}{100} = \frac{50B}{100}$$
or $\frac{B}{A} = \frac{8}{5}$
Now $B = \frac{x \times A}{100} \Rightarrow x = \frac{B}{A} \times 100$

$$\therefore x = \frac{8}{5} \times 100 = 160$$

17. Let numbers =
$$(x-2)$$
, $(x-1)$, $(x+1)$, $(x+2)$

$$\therefore \frac{(x-2)+(x-1)+x+(x+1)+(x+2)}{5} = 7$$

$$\therefore \frac{5x}{5} = 7$$

∴ highest number = 9

$$18. \qquad x^3 + y^3 + z^3 - 3xyz = \big(x + y + z\big)\big(x^2 + y^2 + z^2 - xy - yz - zx\big)$$

Now we know that, $(x + y + z)^2 = x^2 + y^2 + z^2 + 2(xy + yz + zx)$

$$\Rightarrow xy + yz + zx = \frac{15 \times 15 - 51}{2} = 87$$

$$\therefore x^3 + y^3 + z^3 - 3xyz = 15(51 - 87)$$
= 15 × (-36)
= -540

^{:.} Bell rung 20 times.

∴
$$S = \frac{3x + 4x + 5x}{2} = 6x$$

∴ Area = $\sqrt{S(S-a)(S-b)(S-c)}$
 $384 = \sqrt{6x \times 3x \times 2x \times x}$
 $384 = 6x^2$
∴ $x = 8$
∴ $P = 12 \times 8 = 96 \text{ cm}$

20. (1)
$$\frac{1}{3 + \frac{1}{\frac{17}{16}}} = \frac{1}{3 + \frac{16}{17}} = \frac{17}{66}$$

(2)
$$\frac{1}{3 + \frac{1}{1 + \frac{1}{\frac{9}{8}}}} = \frac{1}{3 + \frac{1}{\frac{17}{9}}} = \frac{1}{\frac{60}{17}} = \frac{17}{60}$$

(3)
$$\frac{1}{3 + \frac{1}{1 + \frac{1}{\frac{9}{4}}}} = \frac{1}{3 + \frac{1}{\frac{13}{9}}} = \frac{\frac{1}{48}}{\frac{13}{13}} = \frac{13}{48}$$

$$(4) \qquad \frac{1}{3 + \frac{1}{\frac{9}{8}}} = \frac{1}{\frac{35}{8}} = \frac{8}{35}$$

21.
$$a \$ b = a \times (a + b)$$

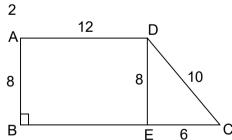
$$\therefore (2 \$ 0) \$ 1 = [2 \times (2 + 0)] \$ 1$$

$$= 4 \$ 1$$

$$= 4 \times (4 + 1)$$

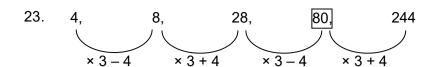
$$= 20$$

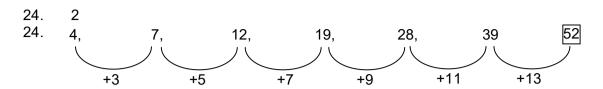
22. 22.



Construction: Draw DE \perp BC

∴ Area of ABCD = Area of rec ABED + Area of
$$\triangle$$
DEC
= $\ell \times b + \frac{1}{2} \times b \times h$
= $8 \times 12 + \frac{1}{2} \times 6 \times 8$
= $96 + 24 = 120 \text{ m}^2$





26. 2
26.
$$CI = P\left[\left(1 + \frac{r}{100}\right)^{n} - 1\right]$$

$$4347 = 30000\left[\left(1 + \frac{7}{100}\right)^{n} - 1\right]$$

$$= \frac{11490}{10000} = \left(\frac{107}{100}\right)^{n}$$

$$= \left(\frac{107}{100}\right)^{2} = \left(\frac{107}{100}\right)^{n}$$

$$\therefore n = 2$$

27. 2
27.
$$2^{\frac{1}{2}}, 9^{\frac{1}{3}}, 16^{\frac{1}{4}}, 32^{\frac{1}{5}}$$

 $= 2^{\frac{1}{2}}, 9^{\frac{1}{3}}, 2^{1}, 2^{1}$
 $= 2^{\frac{6}{2}}, 9^{\frac{6}{3}}, 2^{6}, 2^{6}$
 $= 2^{3}, 9^{2}, 2^{6}, 2^{6}$

28. 3
28.
$$x + \frac{1}{x} = 2$$

 $\Rightarrow x^2 + 1 - 2x = 0$
 $\Rightarrow (x - 1)^2 = 0$
 $\Rightarrow x = 1$
 $\therefore x^{17} + \frac{1}{x^{19}} = 1^{17} + \frac{1}{1^{19}} = 2$

29. 3
29. Let runs required = x
$$\therefore 15 \times 6 + x \times 5 = 7.2 \times 20$$

$$\therefore x = 54$$

$$\therefore \text{ required run rate} = \frac{54}{5} = 10.8$$

30.
$$P + Q = x + y$$
, $PQ = xy$
 $(P + Q)^3 = P^3 + Q^3 = 3PQ (P + Q)$
 $\Rightarrow P^3 + Q^3 = (x + y)^3 - 3xy (x + y) = x^3 + y^3$

31.
$$\frac{x+5}{12} + \frac{x}{16} = 1$$

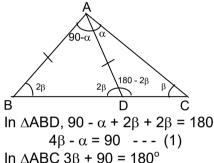
$$= \frac{4x+20+3x}{48} = 1$$

$$\Rightarrow x = \frac{48-20}{7} = \frac{28}{7} = 4$$

$$\therefore x = 4 \text{ min}$$

3

32.



In
$$\triangle ABC 3\beta + 90 = 180^{\circ}$$

$$\Rightarrow \beta = 30$$
 --- (2)

$$\therefore \alpha = 4\beta - 90 = 30^{\circ}$$

Since shaded region has $\frac{1}{6}$ of area of circle 33.

∴
$$\angle$$
 in shaded region = $\frac{360}{6}$ = 60°

∴
$$\angle$$
 in Arc AQB = 360 – 120 = 240

∴ length of arc AQB =
$$360 \times 2\pi r$$

$$=\frac{240}{360}\times2\pi\times10$$

$$=\frac{2}{3}\times 2\pi (10)=\frac{40}{3}\pi$$

34. Let original length = ℓ cm & width = b cm

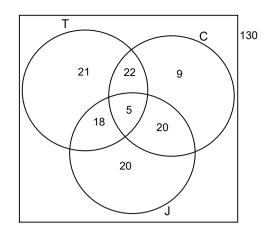
∴ Original Area =
$$\ell$$
bcm²

New area =
$$\frac{125}{100} \ell \times \frac{80}{100} b = \ell b cm^2$$

Since original area = new area

∴ no change in area

35.



- 36. 3 (Incomplete question in English language but according to hindi part it should be 3 (35))
- Let 3 nos = x, y & z36.

$$\therefore x + y = 55 - - - - (1)$$

$$y + z = 65 - - - - (2)$$

$$3x + z = 110 - - - - (3)$$

$$3x + z = 110 - - - - (3)$$

Form eq (1) & (2)

$$55 - x + z = 65$$

$$z - x = 10 - - (4)$$

From eq (3) & (4)
$$3x + z + 3z - 3x = 110 + 30$$

$$z=\frac{140}{4}=35$$

37. For K ratio =
$$\frac{6000}{12000} = \frac{1}{2}$$

For L ratio =
$$\frac{5400}{6000} = \frac{9}{10}$$

For M ratio =
$$\frac{12000}{21000} = \frac{4}{7}$$

For N ratio =
$$\frac{4200}{9000} = \frac{7}{15}$$

For O ratio =
$$\frac{7500}{12000} = \frac{5}{8}$$

Clearly N has the minimum ratio

38. For K ratio =
$$\frac{2400}{27000} = 0.088$$

For L ratio =
$$\frac{1200}{15000}$$
 = 0.08

For M ratio =
$$\frac{4500}{45000}$$
 = 0.10

For N ratio =
$$\frac{2400}{21000}$$
 = 0.114

For O ratio =
$$\frac{3000}{30000}$$
 = 0.10

Clearly N has maximum bonus in comparison to his total income.

39. For K =
$$\frac{12000}{27000} \times 100 = 44.44\%$$

For L = $\frac{6000}{15000} \times 100 = 40\%$
For M = $\frac{21000}{45000} \times 100 = 46.66\%$
For N = $\frac{9000}{21000} \times 100 = 42.85\%$

For O =
$$\frac{12000}{30000} \times 100 = 40\%$$

Clearly M has maximum percentage

40.
$$\frac{6000}{7500} \times 100 = 80\%$$

41.
$$\frac{M}{S} = \frac{4}{5}$$

$$M = 4n, S = 5n$$

$$\frac{\mathsf{M}-\mathsf{5}}{\mathsf{S}-\mathsf{5}}=\frac{\mathsf{7}}{\mathsf{9}}$$

$$\Rightarrow \frac{4n-5}{5n-5} = \frac{7}{9}$$

$$\Rightarrow$$
 36n - 45 = 35n - 35

$$\Rightarrow$$
 n = 10

.. Present ayes are 40 and 50 years.

42. Number of different combinations =
$$3_{C_1} \times 4_{C_1} \times 2_{C_1}$$

$$= \frac{3!}{1! \times 2!} \times \frac{4!}{1! \times 3!} \times \frac{2!}{1! \times 1!} = 4! = 24$$

43. Let original length =
$$\ell$$

And original breadth = b

New area =
$$\frac{112.5 \, \ell}{100} \times \frac{90 \, b}{100}$$

= 1.0125 ℓb

:. Charge in area =
$$\frac{(1.0125 - 1)}{1} \times 100 = 1.25\%$$
 increase

44.
$$x = Even number$$

(1) Odd – Even – 1 = Even
$$\neq$$
 Odd

$$(4)$$
 Odd² + Even² + 1 = Even = Even

$$\ell \times b \times h = \pi r^2 h$$

$$2 \times 10 \times 20 = \pi \times 5^2 \times h$$

$$\therefore h = \frac{400}{25\pi} = \frac{16}{\pi}$$

46.
$$\tan \theta + \omega t \theta = 2$$

$$\tan \theta + \frac{1}{\tan \theta} = 2$$
 ; $\frac{\tan^2 \theta + 1}{\tan \theta} = 2$

$$\Rightarrow$$
 tan² θ – 2 tan θ + 1 = 0

$$\Rightarrow$$
 $(\tan \theta - 1)^2 = 0$

$$\Rightarrow$$
 tan θ = 1

$$\Rightarrow$$
 cot θ = 1.

$$\therefore \tan \theta^{100} + \cot \theta^{100}$$

$$1 + 1 = 2$$

47.
$$(a + b)^4 = \left[(a + b)^2 \right]^2$$

$$= (a^2 + b^2 + 2ab)^2$$

$$= a^4 + b^4 + 4a^2b^2 + 4a^3b + 2a^2b^2 + 4ab^3$$

$$= a^4 + b^4 + 6a^2b^2 + 4a^3b + 4ab^3$$

$$\therefore$$
 Coefficient of $a^2b^2 = 6$.

48.
$$\frac{\text{Girls}}{\text{Total class}} = \frac{x}{x + y}$$

$$64^{n} - 16^{n}$$

We know that $a^n - b^n$ is always divisible by (a - b)

$$\therefore$$
 64ⁿ – 16ⁿ is divisible by 48.

50.
$$x = 2^1 - 2^{1/3} + 2^{2/3}$$

$$x - 2 = 2^{2/3} - 2^{1/3}$$

Cubing both sides

$$x^3 - 8 - 3(2x)(x - 2) = 2^2 - 2^1 - 3(2)(x - 2)$$

$$\Rightarrow$$
 $x^3 - 8 - 6x^2 + 12x = 4 - 2 - 6x + 12$

$$\Rightarrow x^3 - 6x^2 + 18x = 22$$

$$\Rightarrow$$
 $x^3 - 6x^2 + 18x + 18 = 40$

51. 1 figure
$$\Delta s = 6$$

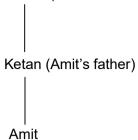
2 figure
$$\Delta s = 4$$

3 figure
$$\Delta s = 2$$

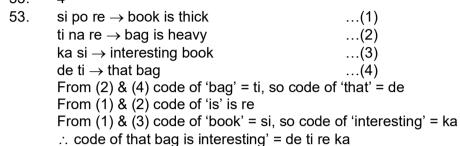
$$\therefore$$
 Total number of $\Delta s = 12$

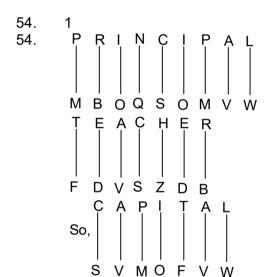


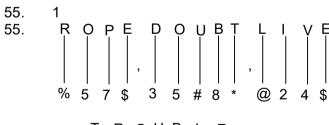




53. 4









61.
$$(9-3) = 6, (6-1) = 5, (5-4) = 1$$

 $(7-5) = 2, (8-4) = 4, (9-3) = 6$
 $\therefore (8-2) = 6, (6-4) = 2, (3-1) = 2$
 $\therefore 622$

62.
$$+ \longrightarrow \div$$

$$- \longrightarrow \times$$

$$\times \longrightarrow +$$

$$\div \longrightarrow -$$

$$\therefore 4 + 6 \times 9 \div 6 - 2 \times 5$$

$$= 4 \div 6 + 9 - 6 \times 2 + 5$$

$$= \frac{2}{3} + 9 - 12 + 5 = \frac{2}{3} + 2$$

$$= \frac{8}{3}$$

```
66. As per observation
```

67.
$$13^2 - 4^2 = 153$$

 $11^2 - 1^2 = 120$
Similarly $6^2 - 2^2 = 32$

68. Total number of Biharis =
$$2 + 1 + 3 = 6$$

69. Total number of Punjabis =
$$1 + 7 + 3 + 5 + 6 = 22$$

70. Total number of Marathis =
$$3 + 6 + 4 + 8 = 21$$

72. Punjabis who are not Marathis =
$$5 + 1 + 7 = 13$$

74.
$$|12 \times 30 - 48 \times 5.5| = 96$$

 \therefore Larger angle = 360 - 96
= 264

75.
$$23\frac{40}{60}$$
 hrs of faulty clock = 24 hrs of actual clock or $\frac{71}{3}$ hrs of faulty clock = 24 hrs of actual clock

∴ 71 hrs of faulty clock =
$$\frac{24 \times 71}{71} \times 3$$

77. Here,
$$\Lambda = 4$$
 Clearly corner (8) cubes are 3 face coloured.

78.
$$12(n-2) = 24$$

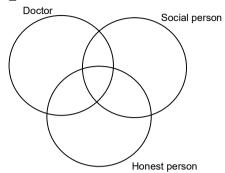
- 79. 2
- 79. $6(n-2)^2 = 24$
- 80. 3
- 80. $4 \times 7 = 28$

$$3 \times 15 = 45$$

Similarly $2 \times 5 = 10$

Logic of letter → In every row A, B & C are present.

- 81. 2
- 81.



- 82. 2
- 82. (1) Difference between B & Q = 15.
 - (2) Difference between D & Y = 21.
 - (3) Difference between U & F = 15
 - (4) Difference between V & E = 17
- 83.
- 83. In given sequence PO & in alphabetical order it is OP.

В

- 84. 4
- 84. In given series letters between Y & L are 12 which is same as original alphabetical order & letters between L and F are 5 which is same as original alphabetical order.
- 85.
- 85. A _____B

Clearly B is the aunt of S.

- l Daughter——R⁺
- 86. No option correct
- 86. Sohan and Neeraj have no mentioned correlation with Abhay, Neena & Sunita.
- 87. 3 87. 18 – 10 = 8

$$18 - 10 - 8$$
 $18 - 4 = 14$

$$10 - 4 = 6$$

Similarly 15 - 5 = 10

- 88. 2
- 88. As per observation.
- 89. 1
- 89. As per observation.
- 90. 3
- 90. Horizontal lines = 3

Vertical lines = 5

Other lines = 8

Total number of lines required = 16

91. 3

Here, n = 4. 91.

 \therefore Cubes with no surface coloured = $(n-2)^3 = 8$

92.

At least 2 face coloured = 2 face coloured + 3 face coloured 92. $= 12 (n-2)^2 + 8 = 24 + 8 = 32$

93. 1

2 surface painted red = 12(n-2) = 2493.

94. No option correct

94. 3 surface painted with red = corner cubes which are 8 in number.

95.

Number of cubes obtained along each axis = 3 95.

 \therefore Total number of cubes = $3 \times 3 \times 3 = 27$

96.

96.

 $X \rightarrow Father$

 $+ \rightarrow \text{Daughter}$

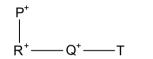
 $\div \rightarrow \mathsf{Mother}$

 $- \rightarrow Brother$

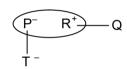
Clearly T is the cousin of P.

97. 4

97. (i)



(ii)



(iii)



(iv)



98.

98.

Clearly R is the son in law of P.



99. 1

99.

Clearly P is the grand mother of T.



100.

100. Clearly Q is the sister of T.