

# Solutions to JEE(Main)-2019

9<sup>th</sup> January 2019(Second Shift)

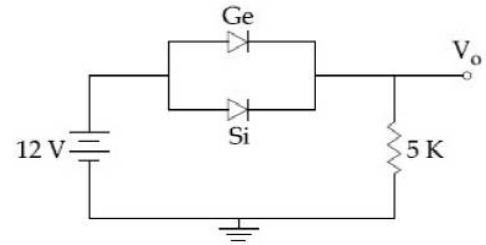
## PART –A (PHYSICS)

1. At a given instant, say  $t = 0$ , two radioactive substances A and B have equal activities. The ratio  $\frac{R_B}{R_A}$  of their activities. The ratio  $\frac{R_B}{R_A}$  of their activities after time  $t$  itself decays with time  $t$  as  $e^{-3t}$ . If the half-life of A is  $\ln 2$ , the half-life of B is:
- (A)  $4\ln 2$  (B)  $\frac{\ln 2}{2}$   
(C)  $\frac{\ln 2}{4}$  (D)  $2\ln 2$
2. A power transmission line feeds input power at 2300 V to a step down transformer with its primary windings having 4000 turns. The output power is delivered at 230 V by the transformer. If the current in the primary of the transformer is 5A and its efficiency is 90%, the output current would be:
- (A) 50 A (B) 45 A  
(C) 35 A (D) 25 A
3. The energy associated with electric field is ( $U_E$ ) and with magnetic field is ( $U_B$ ) for an electromagnetic wave in free space. Then:
- (A)  $U_E = \frac{U_B}{2}$  (B)  $U_E > U_B$   
(C)  $U_E < U_B$  (D)  $U_E = U_B$
4. A force acts on a 2 kg object so that its position is given as a function of time as  $x = 3t^2 + 5$ . What is the work done by this force in first 5 seconds?
- (A) 850 J (B) 950 J  
(C) 875 J (D) 900 J
5. A particle having the same charge as of electron moves in a circular path of radius 0.5 cm under the influence of a magnetic field of 0.5 T. If an electric field of 100 V/m makes it to move in a straight path, then the mass of the particle is (given charge of electron =  $1.6 \times 10^{-19}$  C)
- (A)  $9.1 \times 10^{-31}$  kg (B)  $1.6 \times 10^{-27}$  kg  
(C)  $1.6 \times 10^{-19}$  kg (D)  $2.0 \times 10^{-24}$  kg
6. Two point charges  $q_1(\sqrt{10} \mu\text{C})$  and  $q_2(-25 \mu\text{C})$  are placed on the x-axis at  $x = 1$  m and  $x = 4$  m respectively. The electric field (in V/m) at a point  $y = 3$  m on y-axis is,
- [take  $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{Nm}^2\text{C}^{-2}$ ]
- (A)  $(63\hat{i} - 27\hat{i}) \times 10^2$  (B)  $(-63\hat{i} + 27\hat{i}) \times 10^2$   
(C)  $(81\hat{i} - 81\hat{i}) \times 10^2$  (D)  $(-81\hat{i} + 81\hat{i}) \times 10^2$

7. Expression for time in terms of  $G$  (universal gravitational constant),  $h$  (Planck constant) and  $c$  (speed of light) is proportional to:

(A)  $\sqrt{\frac{hc^5}{G}}$  (B)  $\sqrt{\frac{c^3}{Gh}}$   
 (C)  $\sqrt{\frac{Gh}{c^5}}$  (D)  $\sqrt{\frac{Gh}{c^3}}$

8. Ge and Si diodes start conducting at 0.3 V and 0.7 V respectively. In the following figure if Ge diode connection are reversed, the value of  $V_o$  changes by: (assume that the Ge diode has large breakdown voltage)



- (A) 0.8 V  
 (B) 0.6 V  
 (C) 0.2 V  
 (D) 0.4 V

9. The top of a water tank is open to air and its water level is maintained. It is giving out  $0.74 \text{ m}^3$  water per minute through a circular opening of 2 cm radius in its wall. The depth of the centre of the opening from the level of water in the tank is close to:

- (A) 6.0 m (B) 4.8 m  
 (C) 9.6 m (D) 2.9 m

10. The energy required to take a satellite to a height ' $h$ ' above Earth surface (radius of Earth =  $6.4 \times 10^3 \text{ km}$ ) is  $E_1$  and kinetic energy required for the satellite to be in a circular orbit at this height is  $E_2$ . The value of  $h$  for which  $E_1$  and  $E_2$  are equal is

- (A)  $1.6 \times 10^3 \text{ km}$  (B)  $3.2 \times 10^3 \text{ km}$   
 (C)  $6.4 \times 10^3 \text{ km}$  (D)  $1.28 \times 10^4 \text{ km}$

11. Two Carnot engines A and B are operated in series. The first one, A, receives heat at  $T_1 (= 600 \text{ K})$  and rejects to a reservoir at temperature  $T_2$ . The second engine B receives heat rejected by the first engine and, in turns, rejects to a heat reservoir at  $T_3 (= 400 \text{ K})$ . Calculate the temperature  $T_2$  if the work outputs of the two engines are equal:

- (A) 600 K (B) 400 K  
 (C) 300 K (D) 500 K

12. A series AC circuit containing an inductor (20 mH), a capacitor (120  $\mu\text{F}$ ) and a resistor (60  $\Omega$ ) is driven by an AC source of 24 V/50 Hz. The energy dissipated in the circuit in 60 s is:

- (A)  $5.65 \times 10^2 \text{ J}$  (B)  $2.26 \times 10^3 \text{ J}$   
 (C)  $5.17 \times 10^2 \text{ J}$  (D)  $3.39 \times 10^3 \text{ J}$

13. A particle is executing simple harmonic motion (SHM) of amplitude  $A$ , along the  $x$ -axis, about  $x = 0$ . When its potential energy (PE) equals kinetic energy (KE), the position of the particle will be

- (A)  $\frac{A}{2}$  (B)  $\frac{A}{2\sqrt{2}}$   
 (C)  $\frac{A}{\sqrt{2}}$  (D)  $A$

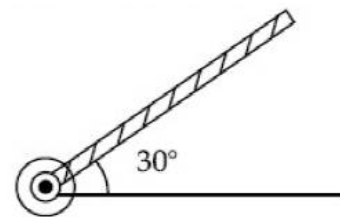
14. A mass of 10 kg is suspended vertically by a rope from the roof. When a horizontal force is applied on the rope at some point, the rope deviated at an angle of  $45^\circ$  at the roof point. If the suspended mass is at equilibrium, the magnitude of the force applied is ( $g = 10 \text{ ms}^{-2}$ )
- (A) 200 N (B) 140 N  
(C) 70 N (D) 100 N

15. A 15 g mass of nitrogen gas is enclosed in a vessel at a temperature  $27^\circ\text{C}$ . Amount of heat transferred to the gas, so that rms velocity of molecules is doubled, is about: [Take  $R = 8.3 \text{ J/K mole}$ ]
- (A) 0.9 kJ (B) 6 kJ  
(C) 10 kJ (D) 14 kJ

16. In a Young's double slit experiment, the slits are placed 0.320 mm apart. Light of wavelength  $\lambda = 500 \text{ nm}$  is incident on the slits. The total number of bright fringes that are observed in the angular range  $-30^\circ \leq \theta \leq 30^\circ$  is:
- (A) 640 (B) 320  
(C) 321 (D) 641

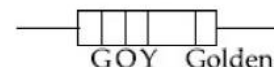
17. Two plane mirrors are inclined to each other such that a ray of light incident to the first mirror ( $M_1$ ) and parallel to the second mirror ( $M_2$ ) is finally reflected from the second mirror ( $M_2$ ) parallel to the first mirror ( $M_1$ ). The angle between the two mirrors will be:
- (A)  $45^\circ$  (B)  $60^\circ$   
(C)  $75^\circ$  (D)  $90^\circ$

18. A rod of length 50 cm is pivoted at one end. It is raised such that it makes an angle of  $30^\circ$  from the horizontal as shown and released from rest. Its angular speed when it passes through the horizontal (in  $\text{rad s}^{-1}$ ) will be ( $g = 10 \text{ ms}^{-2}$ ).



- (A)  $\sqrt{\frac{30}{2}}$  (B)  $\sqrt{30}$   
(C)  $\sqrt{\frac{20}{2}}$  (D)  $\frac{\sqrt{30}}{2}$

19. A carbon resistance has a following colour code. What is the value of the resistance?



- (A)  $530 \text{ k}\Omega \pm 5\%$  (B)  $5.3 \text{ M}\Omega \pm 5\%$   
(C)  $6.4 \text{ M}\Omega \pm 5\%$  (D)  $64 \text{ k}\Omega \pm 10\%$
20. One of the two identical conducting wires of length  $L$  is bent in the form of a circular loop and the other one into a circular coil of  $N$  identical turns. If the same current is passed in both, the ratio of the magnetic field at the central of the loop ( $B_L$ ) to that at the centre of the coil ( $B_C$ ), i.e.  $\frac{B_L}{B_C}$  will be

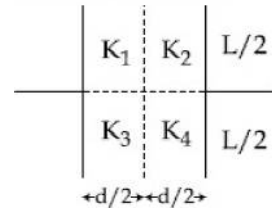
- (A)  $N$  (B)  $\frac{1}{N}$   
(C)  $N^2$  (D)  $\frac{1}{N^2}$

21. A rod of mass 'M' and length '2L' is suspended at its middle by a wire. It exhibits torsional oscillations; If two masses each of 'm' are attached at distance 'L/2' from its centre on both sides, it reduces the oscillation frequency by 20%. The value of ratio m/M is close to:
- (A) 0.77 (B) 0.57  
(C) 0.37 (D) 0.17

22. Charge is distributed within a sphere of radius R with a volume charge density  $\rho(r) = \frac{A}{r^2} e^{-2r/a}$ , where A and a are constants. If Q is the total charge of this charge distribution, the radius R is:

(A)  $a \log \left( 1 - \frac{Q}{2\pi a A} \right)$  (B)  $\frac{a}{2} \log \left( \frac{1}{1 - \frac{Q}{2\pi a A}} \right)$   
(C)  $\frac{a}{2} \log \left( \frac{1}{1 - \frac{Q}{2\pi a A}} \right)$  (D)  $\frac{a}{2} \log \left( 1 - \frac{1}{2\pi a A} \right)$

23. A parallel plate capacitor with square plates is filled with four dielectrics of dielectric constants  $K_1, K_2, K_3, K_4$  arranged as shown in the figure. The effective dielectric constant K will be:



(A)  $K = \frac{(K_1 + K_3)(K_2 + K_4)}{K_1 + K_2 + K_3 + K_4}$  (B)  $K = \frac{(K_1 + K_2)(K_3 + K_4)}{2(K_1 + K_2 + K_3 + K_4)}$   
(C)  $K = \frac{(K_1 + K_2)(K_3 + K_4)}{K_1 + K_2 + K_3 + K_4}$  (D)  $K = \frac{(K_1 + K_4)(K_2 + K_3)}{2(K_1 + K_2 + K_3 + K_4)}$

24. The pitch and the number of divisions, on the circular scale, for a given screw gauge are 0.5 mm and 100 respectively. When the screw gauge is fully tightened without any object, the zero of its circular scale lies 3 divisions below the mean line. The readings of the main scale and the circular scale for a thin sheet, are 5.5 mm and 48 respectively, the thickness of this sheet is
- (A) 5.755 mm (B) 5.950 mm  
(C) 5.725 mm (D) 5.740 mm

25. A musician using an open flute of length 50 cm produces second harmonic sound waves. A person runs towards the musician from another end of a hall at a speed of 10 km/h. If the wave speed is 330 m/s, the frequency heard by the running person shall be close to:
- (A) 666 Hz (B) 753 Hz  
(C) 500 Hz (D) 333 Hz

26. In a car race on straight road, car A takes a time 't' less than car B at the finish and passes finishing point with a speed 'v' more than that of car B. Both the cars start from rest and travel with constant acceleration  $a_1$  and  $a_2$  respectively. Then 'v' is equal to

(A)  $\frac{2a_1 a_2}{a_1 + a_2} t$  (B)  $\sqrt{2a_1 a_2} t$   
 (C)  $\sqrt{a_1 a_2} t$  (D)  $\frac{a_1 + a_2}{2} t$

27. The magnetic field associated with a light wave is given, at the origin, by

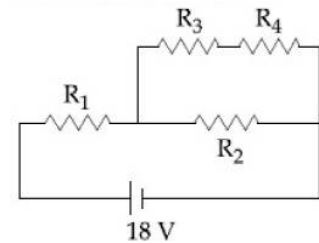
$$B = B_0 [\sin(3.14 \times 10^7)ct + \sin(6.28 \times 10^7)ct]$$

If this light falls on a silver plate having a work function of 4.7 eV, what will be the maximum kinetic energy of the photo electrons?

(A) 6.82 eV (B) 12.5 eV  
 (C) 8.52 eV (D) 7.72 eV

28. In the given circuit the internal resistance of the 18 V cell is negligible. If  $R_1 = 400 \Omega$ ,  $R_3 = 100 \Omega$  and  $R_4 = 500 \Omega$  and the reading of an ideal voltmeter across  $R_4$  is 5 V, then the value of  $R_2$  will be

(A) 300  $\Omega$  (B) 450  $\Omega$   
 (C) 550  $\Omega$  (D) 230  $\Omega$



29. In a communication system operating at wavelength 800 nm, only one percent of source frequency is available as signal bandwidth. The number of channels accommodated for transmitting TV signals of band width 6 MHz are (Take velocity of light  $c = 3 \times 10^8$  m/s,  $h = 6.6 \times 10^{-34}$  J-s)

(A)  $3.75 \times 10^6$  (B)  $3.86 \times 10^6$   
 (C)  $6.25 \times 10^5$  (D)  $4.87 \times 10^5$

30. The position co-ordinates of a particle moving in a 3-D coordinates system is given by

$$x = a \cos \omega t$$

$$y = a \sin \omega t$$

and  $z = a \omega t$

The speed of the particle is:

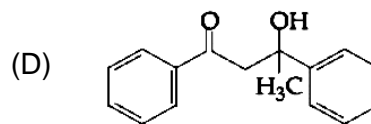
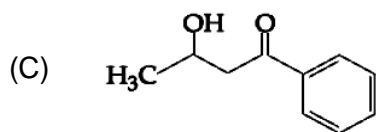
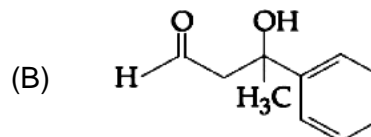
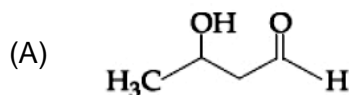
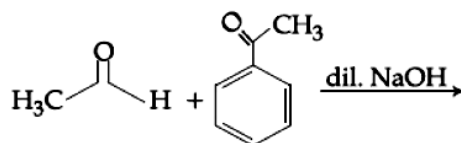
(A)  $\sqrt{2} a \omega$  (B)  $a \omega$   
 (C)  $\sqrt{3} a \omega$  (D)  $2a \omega$

## PART – B (CHEMISTRY)

31. The entropy change associated with the conversion of 1 kg of ice at 273 K to water vapours at 383 K is: (Specific heat of water liquid and water vapours are  $4.2 \text{ kJ K}^{-1} \text{ kg}^{-1}$  and  $2.0 \text{ kJ K}^{-1} \text{ kg}^{-1}$ , heat of liquid fusion and vapourisation of water are  $334 \text{ kJ kg}^{-1}$  and  $2491 \text{ kJ kg}^{-1}$ , respectively) ( $\log 273 = 2.436$ ,  $\log 373 = 2.572$ ,  $\log 383 = 2.583$ )
- (A)  $7.90 \text{ kJ K}^{-1} \text{ kg}^{-1}$  (B)  $2.64 \text{ kJ K}^{-1} \text{ kg}^{-1}$   
 (C)  $8.49 \text{ kJ K}^{-1} \text{ kg}^{-1}$  (D)  $9.26 \text{ kJ K}^{-1} \text{ kg}^{-1}$

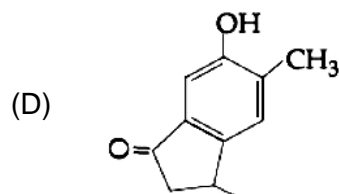
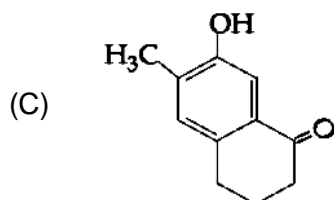
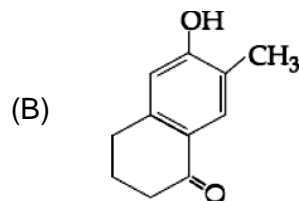
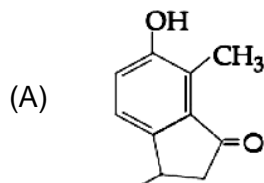
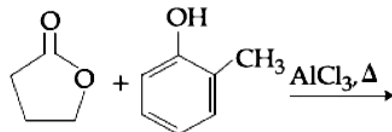
32. For the following reaction the mass of water produced from 445 g of  $\text{C}_{57}\text{H}_{110}\text{O}_6$  is
- $$2\text{C}_{57}\text{H}_{110}\text{O}_6(\text{s}) + 163\text{O}_2(\text{g}) \longrightarrow 114\text{CO}_2(\text{g}) + 110\text{H}_2\text{O}(\text{l})$$
- (A) 490 g (B) 445 g  
 (C) 495 g (D) 890 g

33. The major product formed in the following reaction is:

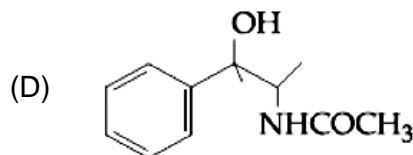
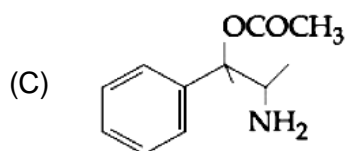
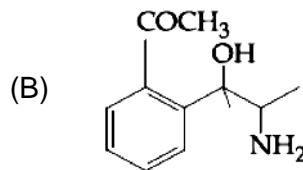
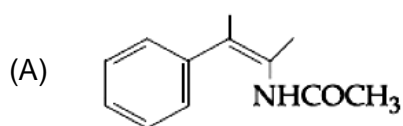
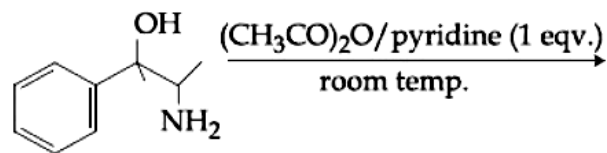


34. Which of the following conditions in drinking water causes methemoglobinemia?
- (A)  $> 50 \text{ ppm}$  of lead (B)  $> 50 \text{ ppm}$  of chloride  
 (C)  $> 50 \text{ ppm}$  of nitrate (D)  $> 100 \text{ ppm}$  of sulphate

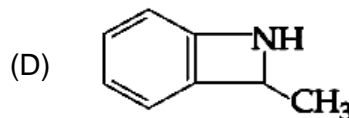
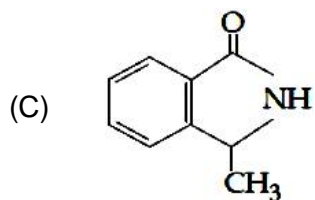
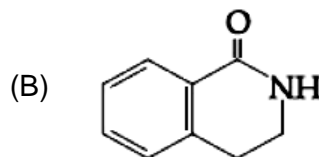
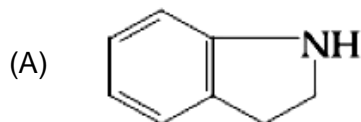
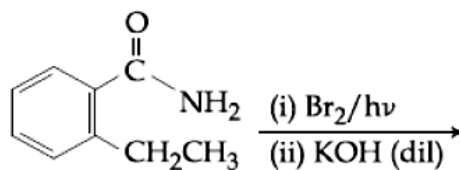
35. The major product of the following reaction is:



36. The major product obtained in the following reaction is:



37. The major product of the following reaction is:



38. The correct match between item I and item II is

- | Item I  | Item II   |
|---|---|
| (a) Benzaldehyde  | (p) Mobile phase  |
| (b) Alumina   | (q) Adsorbent   |
| (c) Acetonitrile  | (r) Adsorbate   |
| (A) a $\rightarrow$ q, b $\rightarrow$ p, c $\rightarrow$ r | (B) a $\rightarrow$ r, b $\rightarrow$ q, c $\rightarrow$ p |
| (C) a $\rightarrow$ q, b $\rightarrow$ r, c $\rightarrow$ p | (D) a $\rightarrow$ p, b $\rightarrow$ r, c $\rightarrow$ q |

39. The metal that forms nitride by reacting directly with  $\text{N}_2$  of air is

- (A) K (B) Li  
(C) Rb (D) Cs

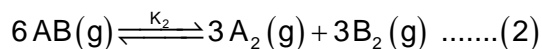
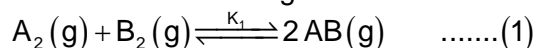
40. For coagulation of arsenious sulphide sol, which one of the following salt solution will be most effective?

- (A)  $\text{BaCl}_2$  (B)  $\text{AlCl}_3$   
(C)  $\text{NaCl}$  (D)  $\text{Na}_3\text{PO}_4$

41. The complex that has highest crystal field splitting energy( $\Delta$ ) is  
 (A)  $[\text{Co}(\text{NH}_3)_5(\text{H}_2\text{O})]\text{Cl}_3$  (B)  $\text{K}_2[\text{CoCl}_4]$   
 (C)  $[\text{Co}(\text{NH}_3)_5\text{Cl}]\text{Cl}_2$  (D)  $\text{K}_3[\text{Co}(\text{CN})_6]$

42. The pH of rain water is approximately  
 (A) 5.6 (B) 7.5  
 (C) 7.0 (D) 6.5

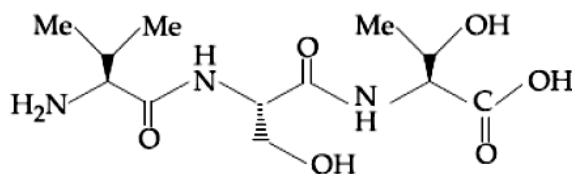
43. Consider the following reversible chemical reactions:



The relation between  $K_1$  and  $K_2$  is

- (A)  $K_1K_2 = \frac{1}{3}$  (B)  $K_2 = K_1^3$   
 (C)  $K_2 = K_1^{-3}$  (D)  $K_1K_2 = 3$

44. The correct sequence of amino acids present in the tripeptide given below is



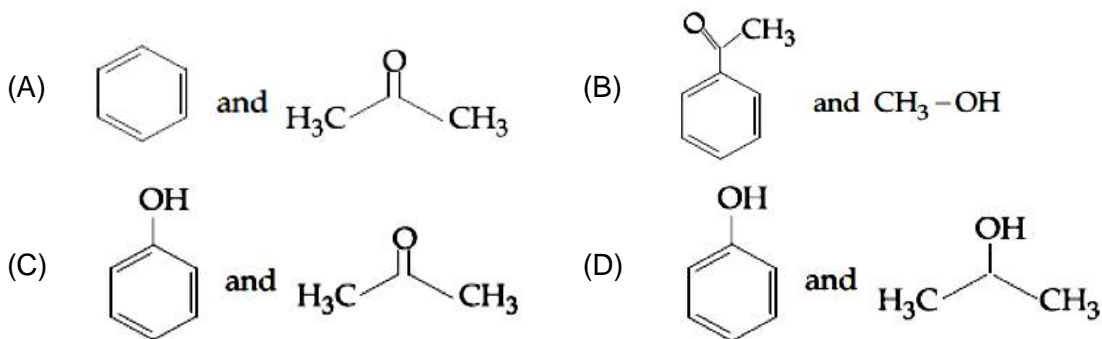
- (A) Val – Ser – Thr (B) Thr – Ser – Val  
 (C) Leu – Ser – Thr (D) Thr – Ser – Leu

45. For the reaction,  $2\text{A} + \text{B} \longrightarrow \text{products}$ , when the concentrations of A and B both were doubled, the rate of the reaction increased from  $0.3 \text{ mol L}^{-1} \text{ s}^{-1}$  to  $2.4 \text{ mol L}^{-1} \text{ s}^{-1}$ . When the concentration of A alone is doubled, the rate increased from  $0.3 \text{ mol L}^{-1} \text{ s}^{-1}$  to  $0.6 \text{ mol L}^{-1} \text{ s}^{-1}$ .

Which one of the following statements is correct?

- (A) Total order of the reaction is 4  
 (B) Order of the reaction with respect to B is 2  
 (C) Order of the reaction with respect to B is 1  
 (D) Order of the reaction with respect to A is 2

46. The products formed in the reaction of cumene with  $\text{O}_2$  followed by treatment with dil. HCl are:

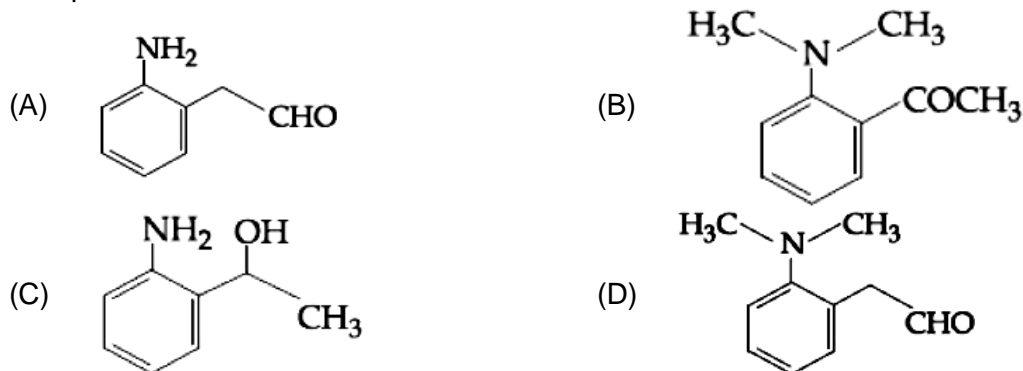




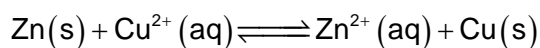
47. The tests performed on compound X and their inferences are:

	Test	Inference
(a)	2, 4-DNP test	Coloured precipitate
(b)	Iodoform test	Yellow precipitate
(c)	Azo-dye test	No dye formation

Compound 'X' is



48. If the standard electrode potential for a cell is 2 V at 300 K, the equilibrium constant (K) for the reaction



At 300 K is approximately

$$(R = 8 \text{ JK}^{-1} \text{ mol}^{-1}, F = 96000 \text{ C mol}^{-1})$$

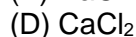
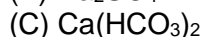
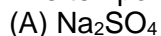
(A)  $e^{-80}$

(B)  $e^{-160}$

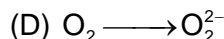
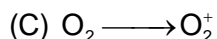
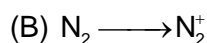
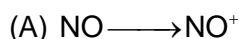
(C)  $e^{320}$

(D)  $e^{160}$

49. The temporary hardness of water is due to



50. In which of the following processes, the bond order has increased and paramagnetic character has changed to diamagnetic?



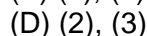
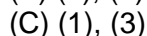
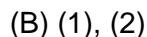
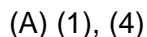
51. Which of the following combination of statements is true regarding the interpretation of the atomic orbitals?

(1) An electron in an orbital of high angular momentum stays away from the nucleus than an electron in the orbital of lower angular momentum.

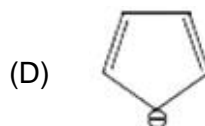
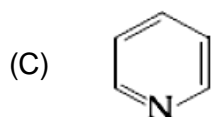
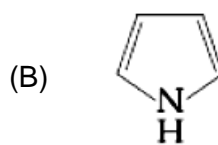
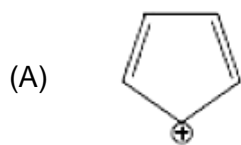
(2) For a given value of the principal quantum number, the size of the orbit is inversely proportional to the azimuthal quantum number

(3) According to wave mechanics, the ground state angular momentum is equal to  $\frac{h}{2\pi}$

(4) The plot of  $\psi$  Vs  $r$  for various azimuthal quantum numbers, shows peak shifting towards higher  $r$  value

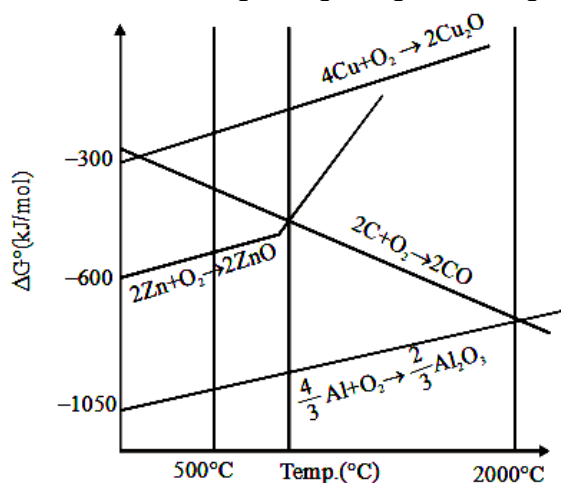


52. Which of the following compounds is not aromatic?



53. Good reducing nature of  $\text{H}_3\text{PO}_2$  is attributed to the presence of  
 (A) Two P – OH bonds (B) One P – H bond  
 (C) Two P – H bonds (D) One P – OH bond

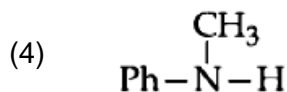
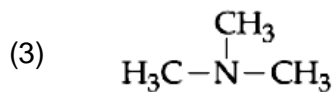
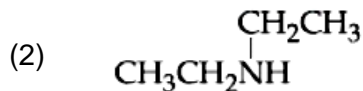
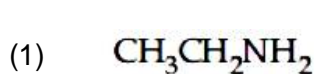
54. The correct statement regarding the given Ellingham diagram is



(A) At  $1400^\circ\text{C}$ , Al can be used for the extraction of Zn from ZnO  
 (B) At  $500^\circ\text{C}$ , coke can be used for the extraction of Zn from ZnO  
 (C) Coke cannot be used for the extraction of Cu from  $\text{Cu}_2\text{O}$   
 (D) At  $800^\circ\text{C}$  Cu can be used for the extraction of Zn from ZnO

55. The transition element that has lowest enthalpy of atomisation is  
 (A) Fe (B) Cu  
 (C) V (D) Zn

56. The increasing basicity order of the following compounds is



(A) (4) < (3) < (2) < (1)  
 (C) (1) < (2) < (3) < (4)

(B) (4) < (3) < (1) < (2)  
 (D) (1) < (2) < (4) < (3)

57. When the first electron gain enthalpy ( $\Delta_{eg}H$ ) of oxygen is  $-141 \text{ kJ/mol}$ , its second electron gain enthalpy is  
 (A) a more negative value than the first (B) almost the same as that of the first  
 (C) negative, but less negative than the first (D) a positive value
58. At  $100^\circ\text{C}$ , copper(Cu) has FCC unit cell structure with cell edge length  $x \text{ \AA}$ . What is the approximate density of Cu(in  $\text{g cm}^{-3}$ ) at this temperature?  
 [Atomic mass of Cu =  $63.55 \text{ u}$ ]  
 (A)  $\frac{205}{x^3}$  (B)  $\frac{105}{x^3}$   
 (C)  $\frac{211}{x^3}$  (D)  $\frac{422}{x^3}$
59. A solution containing  $62 \text{ g}$  ethylene glycol in  $250 \text{ g}$  water is cooled to  $-10^\circ\text{C}$ . If  $K_f$  for water is  $1.86 \text{ K kg mol}^{-1}$ , the amount of water(in  $\text{g}$ ) separated as ice is  
 (A) 48 (B) 32  
 (C) 64 (D) 16
60. Homoleptic octahedral complexes of a metal ion ' $M^{3+}$ ' with three monodentate ligands  $L_1$ ,  $L_2$  and  $L_3$  absorb wavelengths in the region of green, blue and red respectively. The increasing order of the ligand strength is  
 (A)  $L_3 < L_1 < L_2$  (B)  $L_3 < L_2 < L_1$   
 (C)  $L_1 < L_2 < L_3$  (D)  $L_2 < L_1 < L_3$

## PART-C (MATHEMATICS)

61. The sum of the following series  
 $1 + 6 + \frac{9(1^2 + 2^2 + 3^2)}{7} + \frac{12(1^2 + 2^2 + 3^2 + 4^2)}{9} + \frac{15(1^2 + 2^2 + \dots + 5^2)}{11} + \dots$  up to 15 terms, is:  
(A) 7820 (B) 7830  
(C) 7520 (D) 7510
62. For each  $x \in \mathbb{R}$ , let  $[x]$  be the greatest integer less than or equal to  $x$ . Then  
 $\lim_{x \rightarrow 0^+} \frac{x([x] + |x|)\sin[x]}{|x|}$  is equal to  
(A)  $-\sin 1$  (B) 0  
(C) 1 (D)  $\sin 1$
63. Let  $f: [0,1] \rightarrow \mathbb{R}$  be such that  $f(xy) = f(x)f(y)$  for all  $x, y \in [0,1]$ , and  $f(0) \neq 0$ . If  
 $y = y(x)$  satisfies the differential equation,  $\frac{dy}{dx} = f(x)$  with  $y(0) = 1$ , then  $y\left(\frac{1}{4}\right) + y\left(\frac{3}{4}\right)$  is  
equal to  
(A) 4 (B) 3  
(C) 5 (D) 2
64. If  $x = \sin^{-1}(\sin 10)$  and  $y = \cos^{-1}(\cos 10)$ , then  $y - x$  is equal to:  
(A)  $\pi$  (B)  $7\pi$   
(C) 0 (D) 10
65. If  $0 \leq x < \frac{\pi}{2}$ , then the number of values of  $x$  for which  $\sin x - \sin 2x + \sin 3x = 0$ , is  
(A) 2 (B) 1  
(C) 3 (D) 4
66. Let  $z_0$  be a root of the quadratic equation,  $x^2 + x + 1 = 0$ . If  $z = 3 + 6iz_0^{81} - 3iz_0^{93}$ , then  $\arg z$   
is equal to  
(A)  $\frac{\pi}{4}$  (B)  $\frac{\pi}{3}$   
(C) 0 (D)  $\frac{\pi}{6}$
67. The area of the region  $A \{(x, y) : 0 \leq y \leq x|x| + 1 \text{ and } -1 \leq x \leq 1\}$  in sq. units, is:  
(A)  $\frac{2}{3}$  (B)  $\frac{1}{3}$   
(C) 2 (D)  $\frac{4}{3}$

68. If the system of linear equation  $x - 4y + 7z = g$ ,  $3y - 5z = h$ ,  $-2x + 5y - 9z = k$  is consistent, then:  
 (A)  $g + h + k = 0$  (B)  $2g + h + k = 0$   
 (C)  $g + h + 2k = 0$  (D)  $g + 2h + k = 0$
69. The coefficient of  $t^4$  in the expansion of  $\left(\frac{1-t^6}{1-t}\right)^3$  is  
 (A) 12 (B) 15  
 (C) 10 (D) 14
70. If both the roots of the quadratic equation  $x^2 - 5x + 4 = 0$  are real and distinct and they lie in the interval  $[1, 5]$ , then  $m$  lies in the interval.  
 (A) (4, 5) (B) (3, 4)  
 (C) (5, 6) (D) (-5, -4)
71. Let  $S$  be the set of all triangle in the  $xy - plane$ , each having one vertex at the origin and the other two vertices lie on coordinate axes with integral coordinates. If each triangle in  $S$  has area 50 sq. units, then the number of elements in the set  $S$  is:  
 (A) 9 (B) 18  
 (C) 32 (D) 36
72. Let  $a$ ,  $b$  and  $c$  be the 7<sup>th</sup>, 11<sup>th</sup> and 13<sup>th</sup> terms respectively of a non - constant A.P. If these are also the three consecutive terms of a G.P. then  $\frac{a}{c}$  is equal to:  
 (A)  $\frac{1}{2}$  (B) 4  
 (C) 2 (D)  $\frac{7}{13}$
73. The logical statement  $[\sim(\sim p \vee q) \vee (p \wedge r) \wedge (\sim q \wedge r)]$  is equivalent to:  
 (A)  $(p \wedge r) \wedge \sim q$  (B)  $(\sim p \wedge \sim q) \wedge r$   
 (C)  $\sim p \vee r$  (D)  $(p \wedge \sim q) \vee r$
74. The equation of the plane containing the straight line  $\frac{x}{2} = \frac{y}{3} = \frac{z}{4}$  and perpendicular to the plane containing the straight lines  $\frac{x}{3} = \frac{y}{4} = \frac{z}{2}$  and  $\frac{x}{4} = \frac{y}{2} = \frac{z}{3}$  is:  
 (A)  $x + 2y - 2z = 0$  (B)  $x - 2y + z = 0$   
 (C)  $5x + 2y - 4z = 0$  (D)  $3x + 2y - 3z = 0$
75. A data consists of  $n$  observations:  
 $x_1, x_2, \dots, x_n$ . If  $\sum_{i=1}^n (x_i + 1)^2 = 9n$  and  $\sum_{i=1}^n (x_i - 1)^2 = 5n$ , then the standard deviation of this data is:  
 (A) 5 (B)  $\sqrt{5}$   
 (C)  $\sqrt{7}$  (D) 2

76. If  $A = \begin{bmatrix} e^t & e^{-t} \cos t & e^{-t} \sin t \\ e^t & -e^{-t} \cos t - e^{-t} \sin t & -e^{-t} \sin t + e^{-t} \cos t \\ e^t & 2e^{-t} \sin t & -2e^{-t} \cos t \end{bmatrix}$  Then A is
- (A) Invertible only if  $t = \frac{\pi}{2}$  (B) not invertible for any  $t \in \mathbb{R}$   
 (C) invertible for all  $t \in \mathbb{R}$  (D) invertible only if  $t = \pi$
77. If  $f(x) = \int \frac{5x^8 + 7x^6}{(x^2 + 1 + 2x^7)^2} dx, (x \geq 0)$  and  $f(0) = 0$ , then the value of  $f(1)$  is:
- (A)  $-\frac{1}{2}$  (B)  $\frac{1}{2}$   
 (C)  $-\frac{1}{4}$  (D)  $\frac{1}{4}$
78. Let  $f$  be a differentiable function  $\mathbb{R}$  to  $\mathbb{R}$  such that  $|f(x) - f(y)| \leq 2|x - y|^{\frac{3}{2}}$ , for all  $x, y \in \mathbb{R}$ .  
 If  $f(0) = 1$  then  $\int_0^1 f^2(x) dx$  is equal to
- (A) 0 (B)  $\frac{1}{2}$   
 (C) 2 (D) 1
79. If  $x = 3 \tan t$  and  $y = 3 \sec t$ , then the value of  $\frac{d^2y}{dx^2}$  at  $t = \frac{\pi}{4}$ , is:
- (A)  $\frac{3}{2\sqrt{2}}$  (B)  $\frac{1}{3\sqrt{2}}$   
 (C)  $\frac{1}{6}$  (D)  $\frac{1}{6\sqrt{2}}$
80. The number of natural numbers less than 7,000 which can be formed by using the digits 0, 1, 3, 7, 9 (repetition of digits allowed) is equal to:
- (A) 250 (B) 374  
 (C) 372 (D) 375
81. If the circles  $x^2 + y^2 - 16x - 20y + 164 = r^2$  and  $(x - 4)^2 + (y - 7)^2 = 36$  intersect at two distinct points, then:
- (A)  $0 < r < 1$  (B)  $1 < r < 11$   
 (C)  $r > 11$  (D)  $r = 11$
82. A hyperbola has its centre at the origin, passes through the point (4, 2) and has transverse axis of length 4 along the  $x$  - axis. Then the eccentricity of the hyperbola is:
- (A)  $\frac{2}{\sqrt{3}}$  (B)  $\frac{3}{2}$   
 (C)  $\sqrt{3}$  (D) 2

83. Let  $A(4, -4)$  and  $B(9,6)$  be points on the parabola  $y^2 = 4x$ . Let  $C$  be chosen on the arc  $AOB$  of the parabola, where  $O$  is the origin, such that the area of  $\triangle ACB$  is maximum. Then, the area (in sq. units) of  $\triangle ACB$ , is:
- (A)  $31\frac{3}{4}$  (B) 32  
 (C)  $30\frac{1}{2}$  (D)  $31\frac{1}{4}$
84. Let the equation of two sides of a triangle be  $3x - 2y + 6 = 0$  and  $4x + 5y - 20 = 0$ . If the orthocentre of this triangle is at  $(1, 1)$ , then the equation of its third side is:
- (A)  $122y - 26x - 1675 = 0$  (B)  $26x + 61y + 1675 = 0$   
 (C)  $122y + 26x + 1675 = 0$  (D)  $26x - 122y - 1675 = 0$
85. An urn contains 5 red and 2 green balls. A ball is drawn at random from the urn. If the drawn ball is green, then a red ball is added to the urn and if the drawn ball is red, then a green ball is added to the urn; the original ball is not returned to the urn. Now, a second ball is drawn at random from it. The probability that the second ball is red, is:
- (A)  $\frac{26}{49}$  (B)  $\frac{32}{49}$   
 (C)  $\frac{27}{49}$  (D)  $\frac{21}{49}$
86. If the lines  $x = ay + b$ ,  $z = cy + d$  and  $x = a'z + b'$ ,  $y = c'z + d'$  are perpendicular, then:
- (A)  $cc' + a + a' = 0$  (B)  $aa' + c + c' = 0$   
 (C)  $ab' + bc' + 1 = 0$  (D)  $bb' + cc' + 1 = 0$
87. Let  $\vec{a} = \hat{i} + \hat{j} + \sqrt{2}\hat{k}$ ,  $\vec{b} = b_1\hat{i} + b_2\hat{j} + \sqrt{2}\hat{k}$  and  $\vec{c} = 5\hat{i} + \hat{j} + \sqrt{2}\hat{k}$  be three vectors such that the projection vector of  $\vec{b}$  on  $\vec{a}$  is  $\vec{a}$ . If  $\vec{a} + \vec{b}$  is perpendicular to  $\vec{c}$ , then  $|\vec{b}|$  is equal to:
- (A)  $\sqrt{22}$  (B) 4  
 (C)  $\sqrt{32}$  (D) 6
88. The number of all possible positive integral values of  $\alpha$  for which the roots of the quadratic equation,  $6x^2 - 11x + \alpha = 0$  are rational numbers is:
- (A) 2 (B) 5  
 (C) 3 (D) 4
89. Let  $A = \{x \in \mathbb{R} : x \text{ is not a positive integer}\}$ . Define a function  $f : A \rightarrow \mathbb{R}$  as  $f(x) = \frac{2x}{x-1}$  then  $f$  is
- (A) injective but not surjective (B) not injective  
 (C) surjective but not injective (D) neither injective nor surjective
90. If  $\int_0^{\frac{\pi}{3}} \frac{\tan \theta}{\sqrt{2k \sec \theta}} d\theta = 1 - \frac{1}{\sqrt{2}}$ , ( $k > 0$ ), then the value of  $k$  is:
- (A) 2 (B)  $\frac{1}{2}$   
 (C) 4 (D) 1

# JEE (Main) – 2019

## ANSWERS

### PART A – PHYSICS

1.	<b>C</b>	2.	<b>B</b>	3.	<b>D</b>	4.	<b>D</b>
5.	<b>D</b>	6.	<b>A</b>	7.	<b>C</b>	8.	<b>D</b>
9.	<b>B</b>	10.	<b>B</b>	11.	<b>D</b>	12.	<b>C</b>
13.	<b>C</b>	14.	<b>D</b>	15.	<b>C</b>	16.	<b>D</b>
17.	<b>B</b>	18.	<b>B</b>	19.	<b>A</b>	20.	<b>D</b>
21.	<b>C</b>	22.	<b>B</b>	23.	<b>A</b>	24.	<b>C</b>
25.	<b>A</b>	26.	<b>C</b>	27.	<b>D</b>	28.	<b>A</b>
29.	<b>C</b>	30.	<b>A</b>				

### PART B – CHEMISTRY

31.	<b>D</b>	32.	<b>C</b>	33.	<b>C</b>	34.	<b>C</b>
35.	<b>C</b>	36.	<b>D</b>	37.	<b>C</b>	38.	<b>B</b>
39.	<b>B</b>	40.	<b>B</b>	41.	<b>D</b>	42.	<b>A</b>
43.	<b>C</b>	44.	<b>A</b>	45.	<b>B</b>	46.	<b>C</b>
47.	<b>B</b>	48.	<b>D</b>	49.	<b>C</b>	50.	<b>A</b>
51.	<b>A</b>	52.	<b>A</b>	53.	<b>C</b>	54.	<b>A</b>
55.	<b>D</b>	56.	<b>B</b>	57.	<b>D</b>	58.	<b>D</b>
59.	<b>C</b>	60.	<b>A</b>				

### PART C – MATHEMATICS

61.	<b>A</b>	62.	<b>A</b>	63.	<b>B</b>	64.	<b>A</b>
65.	<b>A</b>	66.	<b>A</b>	67.	<b>C</b>	68.	<b>B</b>
69.	<b>B</b>	70.	<b>(Bonus)</b>	71.	<b>D</b>	72.	<b>B</b>
73.	<b>A</b>	74.	<b>B</b>	75.	<b>B</b>	76.	<b>C</b>
77.	<b>D</b>	78.	<b>D</b>	79.	<b>D</b>	80.	<b>B</b>
81.	<b>B</b>	82.	<b>A</b>	83.	<b>D</b>	84.	<b>D</b>
85.	<b>B</b>	86.	<b>B</b>	87.	<b>D</b>	88.	<b>C</b>
89.	<b>A</b>	90.	<b>A</b>				



# HINTS AND SOLUTIONS

## PART A—PHYSICS

1.  $R = R_0 e^{-\lambda t}$

$$\therefore \frac{R_B}{R_A} = \frac{R_0 e^{-\lambda_B t}}{R_0 e^{-\lambda_A t}} = e^{-(\lambda_B - \lambda_A)t} = e^{-3t}$$

$$\Rightarrow \lambda_B - \lambda_A = 3$$

$$\Rightarrow \frac{\ln 2}{T_B} - \frac{\ln 2}{\ln 2} = 3.$$

$$\Rightarrow T_B = \frac{\ln 2}{4}$$

2.  $P_s = \eta P_p$

$$\Rightarrow E_s i_s = \eta E_i i_p$$

$$\Rightarrow i_s = \frac{(0.9)(2300)(5)}{(230)} = 45 \text{ A.}$$

3.  $B = \frac{E}{C}$

$$\Rightarrow U_E = \frac{1}{2} \epsilon_0 E^2$$

$$U_B = \frac{B^2}{2\mu_0} = \frac{E^2}{2\mu_0 C^2} = \frac{E^2}{2\mu_0} (\mu_0 \epsilon_0) = U_E$$

4.  $x = 3t^2 + 5$

$$\Rightarrow v = 6t$$

$$\Rightarrow \Delta W = \Delta k$$

$$= \frac{1}{2}(2)(30)^2 - \frac{1}{2}2(0)^2$$

$$= 900 \text{ J}$$

5.  $eE = evB$

$$\Rightarrow E = \left( \frac{eBr}{m} \right) B$$

$$\Rightarrow m = \frac{eB^2 r}{E}$$

$$\Rightarrow m = \frac{(1.6 \times 10^{-19})(0.5)^2 (0.5 \times 10^{-2})}{100} = 2 \times 10^{-24} \text{ kg.}$$

6.  $\vec{E} = \frac{kq_1}{r_1^3} \vec{r}_1 + \frac{kq_2}{r_2^3} \vec{r}_2 = k \times 10^{-6} \left[ \frac{\sqrt{10}}{10\sqrt{10}} (-\hat{i} + 3\hat{j}) + \frac{(-25)}{125} (-4\hat{i} + 3\hat{j}) \right]$

$$= (9 \times 10^3) \left[ \frac{1}{10} (-\hat{i} + 3\hat{j}) - \frac{1}{5} (-4\hat{i} + 3\hat{j}) \right]$$

$$= (9 \times 10^3) \left[ \left( -\frac{1}{10} + \frac{4}{5} \right) \hat{i} + \left( \frac{3}{10} - \frac{3}{5} \right) \hat{j} \right] = 9000 \left( \frac{7}{10} \hat{i} - \frac{3}{10} \hat{j} \right)$$

$$= (63\hat{i} - 27\hat{j}) (100)$$

7.  $t = G^a h^b c^c$

$$\Rightarrow M^0 L^0 T^1 = (M^{-1} L^3 T^{-2})^a (ML^2 T^{-1})^b (LT^{-1})^c$$

$$\Rightarrow -a + b = 0 \Rightarrow a = b$$

$$\Rightarrow 3a + 2b + c = 0$$

$$\Rightarrow c = -5a$$

$$\Rightarrow -2a - b - c = 1$$

$$\Rightarrow a = \frac{1}{2}; b = \frac{1}{2}; c = -\frac{5}{2}$$

8.  $V_{O_i} = 12 - 0.3 = 11.7 \text{ V}$   
 $V_{O_r} = 12 - 0.7 = 11.3 \text{ V}$   
 $\Rightarrow \Delta V_o = -0.4 \text{ V}$

9.  $\frac{dV}{dt} = Av \Rightarrow \frac{dV}{dt} = A\sqrt{2gh}$

$$\Rightarrow \frac{0.74}{60} = (3.14) \left( \frac{2}{100} \right)^2 \sqrt{2(9.8)h}$$

$$\Rightarrow h = 4.92 \text{ m}$$

10.  $E_1 = -\frac{GMm}{R+h} - \left( -\frac{GMm}{R} \right)$

$$E_2 = \frac{1}{2} m \left( \sqrt{\frac{GM}{R+h}} \right)^2 = \frac{GMm}{2(R+h)}$$

$$E_1 = E_2; h = \frac{R}{2}$$

11.  $W_1 = W_2$   
 $\Rightarrow 600 - T_2 = T_2 - 400$   
 $\Rightarrow T_2 = 500 \text{ K}$

12.  $E = Pt = \frac{E^2}{Z^2} Rt = \frac{(24)^2}{60^2 + (8.33\pi - 2\pi)^2} (60)(60) = 518 \text{ J.}$

13.  $PE = KE$

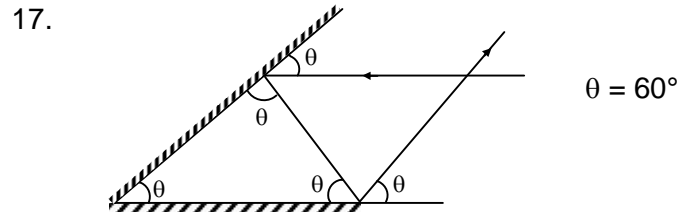
$$\Rightarrow \frac{1}{2} m \omega^2 (A^2 - x^2) = \frac{1}{2} m \omega^2 x^2$$

$$\Rightarrow x = \frac{A}{\sqrt{2}}$$

14.  $T \cos 45^\circ = mg$   
 $T \sin 45^\circ = F$   
 $\Rightarrow F = mg = 100 \text{ N.}$

15.  $\Delta Q = \frac{f}{2} n R \Delta T$   
 $= \frac{5}{2} \left( \frac{15}{28} \right) (8.3) (1200 - 300) = 10000 \text{ J.}$

16.  $\Delta X_{\max} = d \sin \theta = 0.32 \sin 30 = 0.16 \text{ mm}$   
 $\therefore n = \frac{\Delta X_{\max}}{\lambda} = \frac{0.16 \times 10^{-3}}{500 \times 10^{-9}}$   
 $= \frac{0.16 \times 10^6}{500} = \frac{1600}{5} = 320$   
 $\therefore \text{Number of BFs} = (2n + 1) = 641$



18.  $mg \frac{\ell}{2} \left( \frac{1}{2} \right) = \frac{1}{2} \left( \frac{m \ell^2}{3} \right) \omega^2$   
 $\Rightarrow \omega = \sqrt{\frac{3g}{2\ell}} = \sqrt{30}$

19.  $R = 530 \text{ k}\Omega \pm 5\%$

20.  $B_L = \frac{\mu_0 i}{2R}$   
 $B_C = \frac{\mu_0 N i}{2(R/N)}$   
 $\therefore \frac{B_L}{B_C} = \frac{1}{N^2}$

21.  $f = \frac{1}{2\pi} \sqrt{\frac{C}{\left( \frac{ML^2}{3} \right)}} \quad \& \quad 0.8f = \frac{1}{2\pi} \sqrt{\frac{C}{\left( \frac{ML^2}{3} + \frac{mL^2}{2} \right)}}$   
 $\Rightarrow \frac{25}{16} = \frac{\frac{ML^2}{3} + \frac{mL^2}{2}}{\frac{ML^2}{3}}$

$$\Rightarrow \frac{25}{16} = 1 + \frac{3m}{2M}$$

$$\Rightarrow \frac{9}{16} = \frac{3m}{2M}$$

$$\Rightarrow \frac{m}{M} = \frac{3}{8} = 0.37$$

$$\begin{aligned} 22. \quad Q &= \int_0^R \rho 4\pi r^2 dr = \int_0^R \left( \frac{A}{r^2} e^{-\frac{2r}{a}} \right) (4\pi r^2) dr \\ &= 4\pi A \frac{a}{2} \left( 1 - e^{-\frac{2R}{a}} \right) \\ \Rightarrow R &= \frac{-a}{2} \log \left( 1 - \frac{Q}{2\pi A a} \right) \end{aligned}$$

$$23. \quad C_1 = \frac{\epsilon_0 K_1 \frac{L^2}{2}}{\frac{d}{2}} + \frac{\epsilon_0 K_3 \frac{L^2}{2}}{\left(\frac{d}{2}\right)} = \frac{\epsilon_0 L^2}{d} (K_1 + K_3)$$

$$C_2 = \frac{\epsilon_0 K_2 \frac{L^2}{2}}{\frac{d}{2}} + \frac{\epsilon_0 K_4 \frac{L^2}{2}}{\frac{d}{2}} = \frac{\epsilon_0 L^2}{d} (K_2 + K_4)$$

$$\therefore \frac{1}{c} = \frac{1}{c_1} + \frac{1}{c_2}$$

$$\Rightarrow \frac{d}{\epsilon_0 K L^2} = \frac{d}{\epsilon_0 L^2 (K_1 + K_3)} + \frac{d}{\epsilon_0 L^2 (K_2 + K_4)}$$

$$24. \quad \text{Zero error} = 0 + 3 \times \frac{0.5 \text{ mm}}{100} = 0.015 \text{ mm}$$

$$\text{MSR} = 5.5 + 48 \times \frac{0.5}{100}$$

$$= 5.74 \text{ mm.}$$

$$\therefore \text{Thickness} = 5.74 - 0.015 = 5.725 \text{ mm}$$

$$25. \quad f = \frac{2}{2\ell} v_s = \frac{330}{0.5} = 660 \text{ Hz}$$

$$\begin{aligned} \therefore f' &= f \left( \frac{v_s + v}{v_s} \right) = (660) \left( \frac{330 + \frac{50}{18}}{330} \right) = 660 \left( 1 + \frac{50}{18 \times 330} \right) \\ &= 666 \text{ Hz.} \end{aligned}$$

$$26. \quad \sqrt{\frac{2l}{a_2}} - \sqrt{\frac{2l}{a_1}} = t \quad \Rightarrow \quad \frac{\sqrt{2l}}{t} = \frac{\sqrt{a_1 a_2}}{\sqrt{a_1} - \sqrt{a_2}}$$

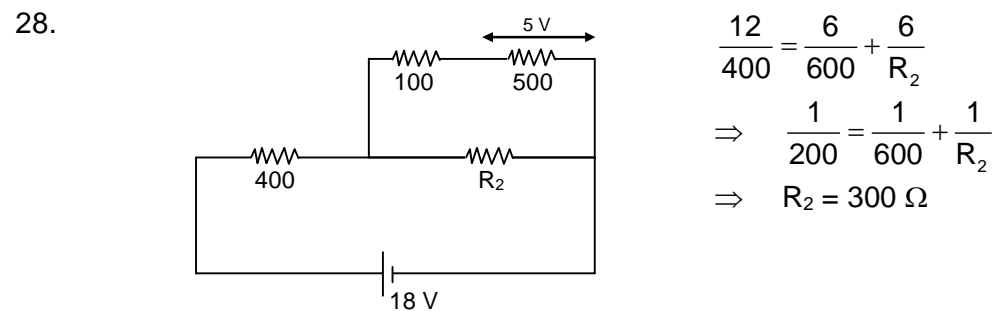
$$\sqrt{2a_1 l} - \sqrt{2a_2 l} = v \quad \Rightarrow \quad \frac{\sqrt{2l}}{v} = \frac{1}{\sqrt{a_1} - \sqrt{a_2}}$$

$$\Rightarrow \quad \frac{v}{t} = \sqrt{a_1 a_2} \quad \Rightarrow \quad v = (\sqrt{a_1 a_2}) t$$

$$27. \quad KE_{\max} = h\nu_{\max} - \phi$$

$$= \frac{(6.6 \times 10^{-34})(6.28 \times 10^7)(3 \times 10^8)}{1.6 \times 10^{-19} \times 2 \times 3.14} - 4.7$$

$$= 12.37 - 4.7 = 7.67 \text{ eV}$$



$$29. \quad f = \frac{c}{\lambda} = \frac{3 \times 10^8}{8 \times 10^{-7}} = \frac{3}{8} \times 10^{15} \text{ Hz}$$

$$\therefore n = \frac{(0.01) f}{6 \times 10^6} = \frac{\frac{3}{8} \times 10^{13}}{6 \times 10^6}$$

$$= \frac{1}{16} \times 10^7 = 6.25 \times 10^5$$

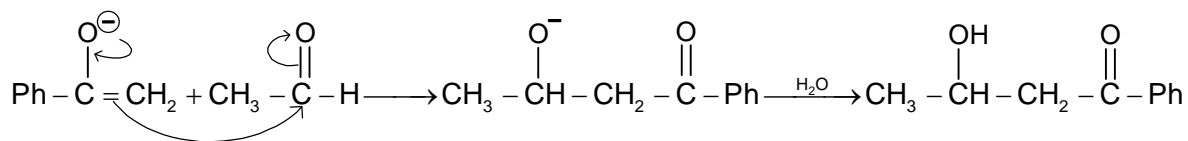
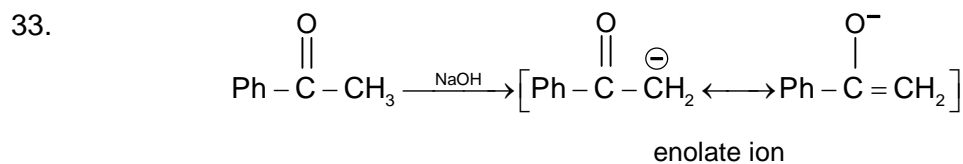
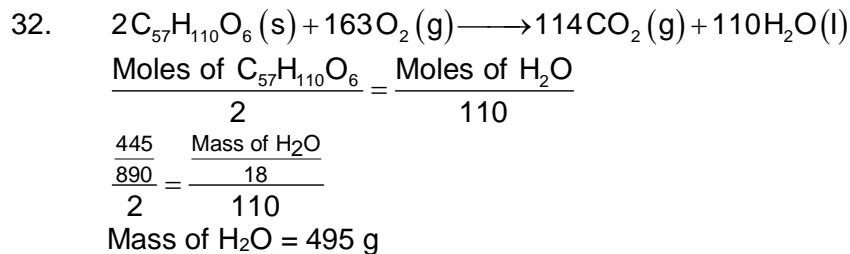
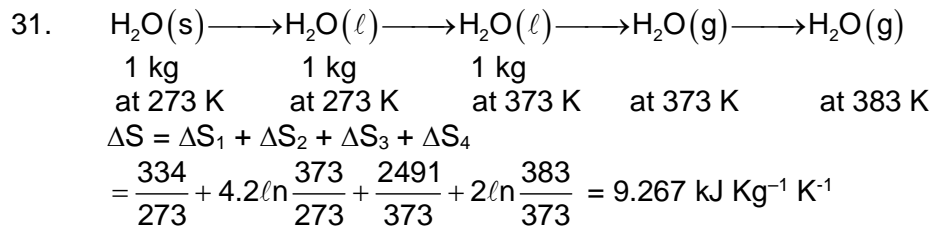
$$30. \quad v_x = \frac{dx}{dt} = -a\omega \sin \omega t$$

$$v_y = \frac{dy}{dt} = a\omega \cos \omega t$$

$$v_z = \frac{dz}{dt} = a\omega$$

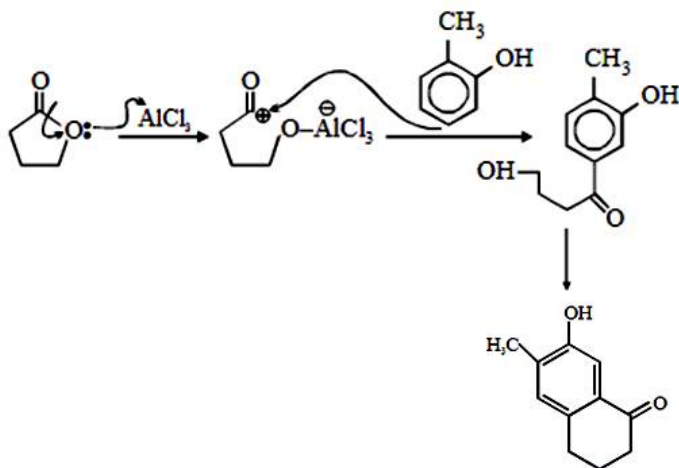
$$\therefore v = \sqrt{v_x^2 + v_y^2 + v_z^2} = a\omega\sqrt{2}$$

## PART B – CHEMISTRY

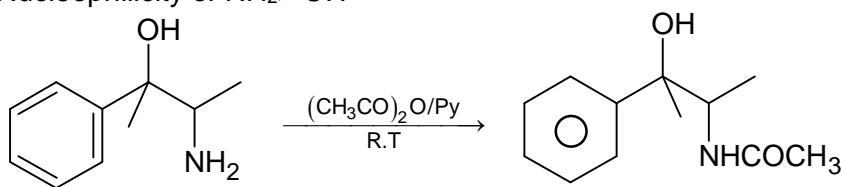


34. Fact based

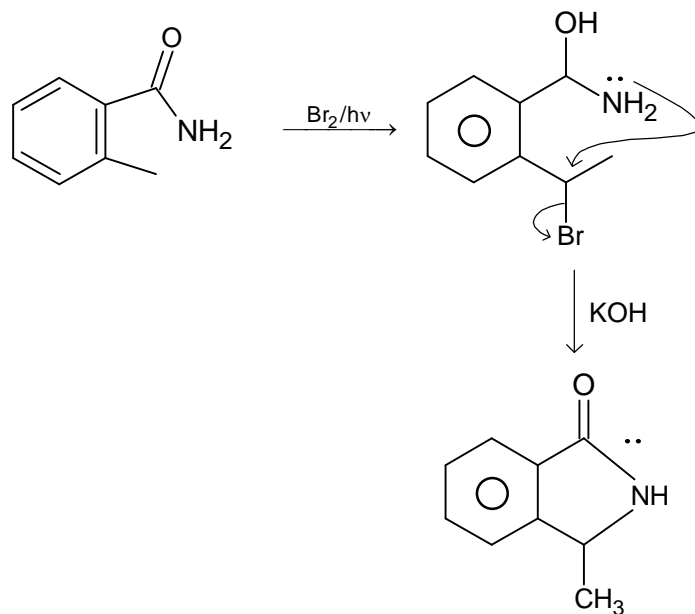
35.



36. Nucleophilicity of  $\text{NH}_2 > \text{OH}$



37.



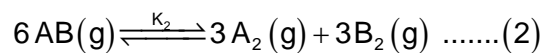
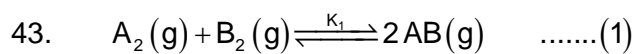
38. Acetonitrile is used as mobile phase for most of the reverse chromatography. Benzaldehyde is adsorbed on alumina.

39. The only alkali metal which forms nitride by reacting directly with  $\text{N}_2$  is 'Li'.

40.  $\text{As}_2\text{S}_3$  is a negatively charged sol. so  $\text{AlCl}_3$  will be most effective.

41. As  $\text{CN}^-$  is a strong field ligand.  $\text{K}_3[\text{Co}(\text{CN})_6]$  will have maximum ' $\Delta$ '.

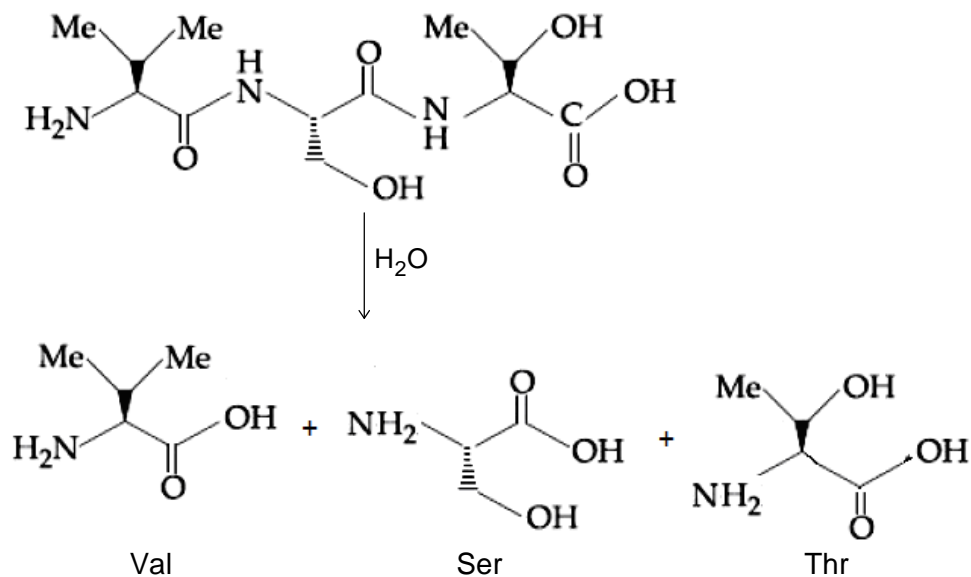
42. Fact based.



Reaction(2) = -3 × reaction(1)

$$\therefore K_2 = \left(\frac{1}{K_1}\right)^3 \Rightarrow K_2 = K_1^{-3}$$

44.

45.  $2A + B \longrightarrow \text{products}$ 

$$\text{Rate} = K[A]^x[B]^y$$

$$r = K[A]^x[B]^y \text{ ---- (i)}$$

$$0.3 = K[A]^x[B]^y \text{ ---- (1)}$$

$$2.4 = K[2A]^x[2B]^y \text{ ---- (2)}$$

$$0.6 = K[2A]^x[B]^y \text{ ---- (3)}$$

From (1), (2) &amp; (3)

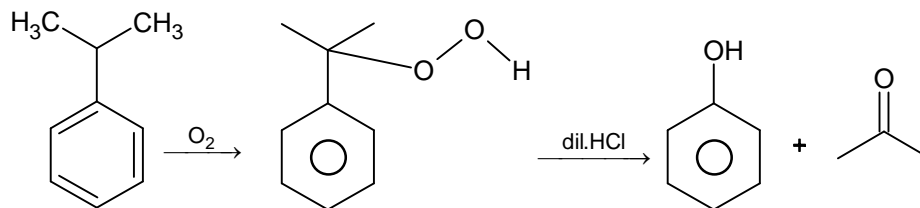
$$x = 1, y = 2$$

$$\text{Overall order} = 2 + 1 = 3$$

$$\text{Order w.r.t A} = 1$$

$$\text{Order w.r.t B} = 2$$

46.

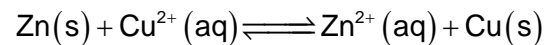


47.

$\therefore -\text{COCH}_3$  is present it will show both 2, 4-DNP & iodoform test.

Due to steric inhibition of resonance. I.P of 'N' is not involved in delocalization so coupling reaction will not take place.

48.



$$-nFE_{\text{cell}} = -RT \ln K$$

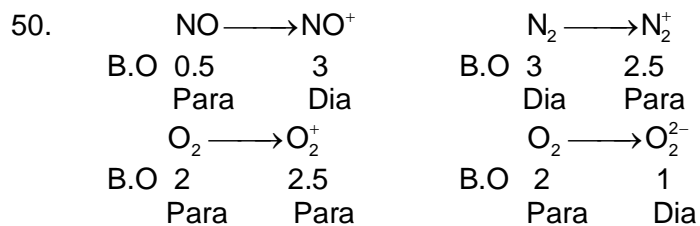
$$\ln K = \frac{2 \times 96500 \times 2}{8 \times 300} = 160.83$$

$$K = e^{160}$$

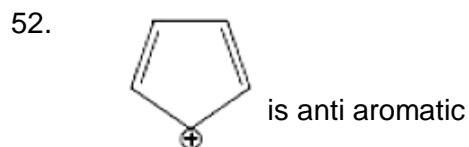
49.

Fact based.

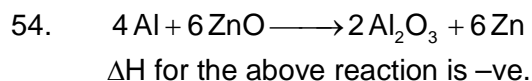




51. Refer Theory



53. Refer theory



55. Due to weak metallic bonding.

56. Correct order of basic strength is  
 $\text{NH}_2(\text{Et})_2 > \text{EtNH}_2 > \text{NMC}_3 > \text{Ph} - \text{NH} - \text{CH}_3$

57. 2<sup>nd</sup> electron gain enthalpy of oxygen is positive.

58. 
$$d = \frac{ZM}{N_a a^3}$$

$$= \frac{4 \times 63.55}{6.023 \times 10^{23} \times (x \times 10^{-8})^3} = \frac{422}{x^3} \text{ gm / cm}^3$$

59. Let moles of H<sub>2</sub>O separated as ice = x gm  
 $\Delta T_f = iK_f m$

$$10 = 1 \times 1.86 \frac{\frac{62}{250-x}}{1000}$$

$$x = 64 \text{ gm}$$

60. L<sub>1</sub>      L<sub>2</sub>      L<sub>3</sub>  
 Green   Blue   Red absorbed wave length  
 Order of  $\lambda$  Red > Green > Blue  
 $L_3 > L_1 > L_2$   
 $\therefore$  Strength of ligand  $\alpha \Delta \propto 1/\lambda$   
 $\therefore$  Strength of ligand  $L_2 > L_1 > L_3$

## PART C – MATHEMATICS

$$61. \quad T_n = \frac{(3 + (n-1) \times 3)(1^2 + 2^2 + \dots + n^2)}{(2n+1)}$$

$$T_n = \frac{3 \cdot \frac{n^2(n+1)(2n+1)}{6}}{2n+1} = \frac{n^2(n+1)}{2}$$

$$S_{15} = \frac{1}{2} \sum_{n=1}^{15} (n^3 + n^2) = \frac{1}{2} \left[ \left( \frac{15(15+1)}{2} \right)^2 + \frac{15 \times 16 \times 31}{6} \right]$$

$$= 7820$$

$$62. \quad \lim_{x \rightarrow 0^+} \frac{x([x] + |x|) \sin[x]}{|x|}$$

$$x \rightarrow 0^-$$

$$\left. \begin{array}{l} [x] = -1 \\ |x| = -x \end{array} \right\} \Rightarrow \lim_{x \rightarrow 0^-} \frac{x(-x-1) \sin(-1)}{-x} = -\sin 1$$

$$63. \quad f(xy) = f(x) \cdot f(y)$$

$$f(0) = 1 \text{ as } f(0) \neq 0$$

$$\Rightarrow f(x) = 1$$

$$\frac{dy}{dx} = f(x) = 1$$

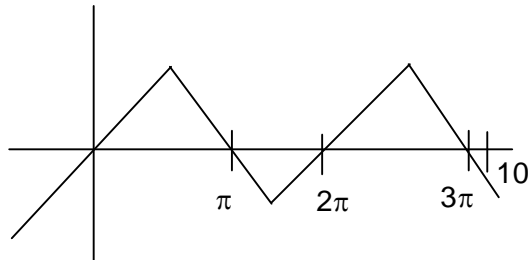
$$\Rightarrow y = x + c$$

$$\text{At, } x=0, y=1 \Rightarrow c=1$$

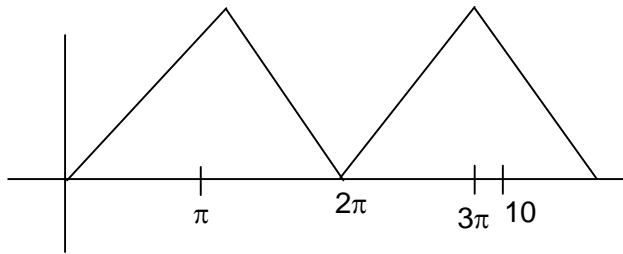
$$y = x + 1$$

$$\Rightarrow y\left(\frac{1}{4}\right) + y\left(\frac{3}{4}\right) = \frac{1}{4} + 1 + \frac{3}{4} + 1 = 3$$

64.



$$x = \sin^{-1}(\sin 10) = 3\pi - 10$$



$$y = \cos^{-1}(\cos 10) = 4\pi - 10$$

$$y - x = \pi$$

65.  $\sin x - \sin 2x + \sin 3x = 0$

$$\Rightarrow (\sin x + \sin 3x) - \sin 2x = 0$$

$$\Rightarrow 2 \sin x \cdot \cos x - \sin 2x = 0$$

$$\Rightarrow \sin 2x(2 \cos x - 1) = 0$$

$$\Rightarrow \sin 2x = 0 \text{ or } \cos x = \frac{1}{2} \Rightarrow x = 0, \frac{\pi}{3}$$

66.  $z_0 = \omega$  or  $\omega^2$  (where  $\omega$  is a non-real cube root of unity)

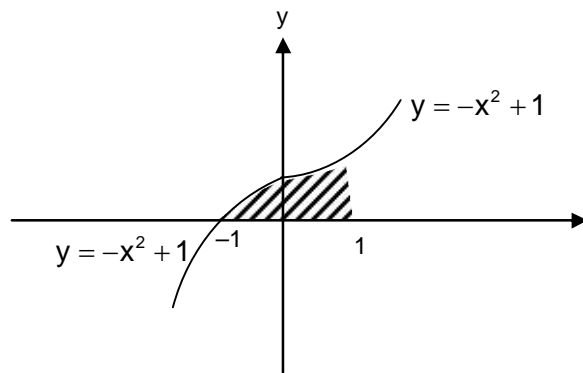
$$z = 3 + 6i(\omega)^{81} - 3i(\omega)^{93}$$

$$z = 3 + 3i$$

$$\Rightarrow \arg z = \frac{\pi}{4}$$

67. The graph is as follows

$$\int_{-1}^0 (-x^2 + 1) dx + \int_0^1 (x^2 + 1) dx = 2$$



68.  $P_1 = x - 4y + 7z - g = 0$

$$P_2 = 3x - 5y - h = 0$$

$$P_3 = -2x + 5y - 9z - k = 0$$

Here  $\Delta = 0$

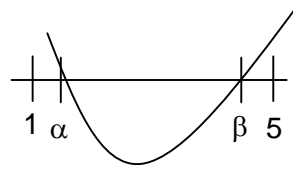
$$2P_1 + P_2 + P_3 = 0 \text{ when } 2g + h + k = 0$$

69.  $(1-t^6)^3 (1-t)^{-3}$

$$(1-t^{18} - 3t^6 + 3t^{12})(1-t)^{-3}$$

$$\Rightarrow \text{coefficient of } t^4 \text{ in } (1-t)^{-3} \text{ is } {}^{3+4-1}C_4 = {}^6C_2 = 15$$

70.  $x^2 - mx + 4 = 0$   
 $\alpha, \beta \in [1, 5]$



- (1)  $D > 0 \Rightarrow m^2 - 16 > 0$   
 $\Rightarrow m \in (-\infty, -4) \cup (4, \infty)$
- (2)  $f(1) \geq 0 \Rightarrow 5 - m \geq 0 \Rightarrow m \in (-\infty, 5]$
- (3)  $f(5) \geq 0 \Rightarrow 29 - 5m \geq 0 \Rightarrow m \in \left(-\infty, \frac{29}{5}\right]$
- (4)  $1 < \frac{-b}{2a} < 5 \Rightarrow 1 < \frac{m}{2} < 5 \Rightarrow m \in (2, 10)$   
 $\Rightarrow m \in (4, 5)$

No option correct : Bonus

\* If we consider  $\alpha, \beta \in (1, 5)$  then option (1) is correct.

71. Let  $A(\alpha, 0)$  and  $B(0, \beta)$  be the vertices of the given triangle AOB

$$\Rightarrow |\alpha\beta| = 100$$

$\Rightarrow$  Number of triangles

$$= 4 \times (\text{number of divisors of } 100)$$

$$= 4 \times 9 = 36$$

72.  $a = A + 6d$

$$b = A + 10d$$

$$c = A + 12d$$

$a, b, c$  are in G.P.

$$\Rightarrow (A + 10d)^2 = (A + 6d)(A + 12d)$$

$$\Rightarrow \frac{A}{d} = -14$$

$$\frac{a}{c} = \frac{A + 6d}{A + 12d} = \frac{6 + \frac{A}{d}}{12 + \frac{A}{d}} = \frac{6 - 14}{12 - 14} = 4$$

73.  $[\sim(\sim p \vee q) \wedge (p \wedge r)] \cap (\sim q \wedge r)$

$$\equiv [(p \wedge \sim q) \vee (p \wedge r)] \wedge (\sim q \wedge r)$$

$$\equiv [p \wedge (\sim q \vee r)] \wedge (\sim q \wedge r)$$

$$\equiv p \wedge (\sim q \wedge r)$$

$$\equiv (p \wedge r) \sim q$$

74. Vector along the normal to the plane containing the lines  $\frac{x}{3} = \frac{y}{4} = \frac{z}{2}$  and  $\frac{x}{4} = \frac{y}{2} = \frac{z}{3}$  is  $(8\hat{i} - \hat{j} - 10\hat{k})$ .

Vector perpendicular to the vectors  $2\hat{i} + 3\hat{j} + 4\hat{k}$  and  $8\hat{i} - \hat{j} - 10\hat{k}$  is  $26\hat{i} - 52\hat{j} + 26\hat{k}$   
 So, required plane is  $26x - 52y + 26z = 0 \Rightarrow x - 2y + z = 0$

75.  $\sum (x_i + 1)^2 = 9n$  .....(1)

$\sum (x_i - 1)^2 = 5n$  .....(2)

(1)+(2)  $\Rightarrow \sum (x_i^2 + 1) = 7n$

$\Rightarrow \frac{\sum x_i^2}{n} = 6$

(1) . (2)  $\Rightarrow 4\sum x_i = 4n$

$\Rightarrow \sum x_i = n$

$\Rightarrow \frac{\sum x_i}{n} = 1$

$\Rightarrow \text{variance} = 6 - 1 = 5$

$\Rightarrow \text{standard deviation} = \sqrt{5}$

76.  $|A| = e^{-t} \begin{vmatrix} 1 & \cos t & \sin t \\ 1 & -\cos t - \sin t & -\sin t + \cos t \\ 1 & 2\sin t & -2\cos t \end{vmatrix}$

$= e^{-t} [5\cos^2 t + 5\sin^2 t] \forall t \in \mathbb{R}$

$= 5e^{-t} \neq 0 \forall t \in \mathbb{R}$

77.  $\int \frac{5x^8 + 7x^6}{(x^2 + 1 + 2x^7)^2} dx$

$= \int \frac{5x^{-6} + 7x^{-8}}{\left(\frac{1}{x^7} + \frac{1}{x^5} + 2\right)^2} dx = \frac{1}{2 + \frac{1}{x^5} + \frac{1}{x^7}} + C$

As  $f(0) = 0$ ,  $f(x) = \frac{x^7}{2x^7 + x^2 + 1}$

$f(1) = \frac{1}{4}$

78.  $|f(x) - f(y)| \leq 2|x - y|^{3/2}$

divide both side by  $|x - y|$

$\left| \frac{f(x) - f(y)}{x - y} \right| \leq 2 \cdot |x - y|^{1/2}$

Apply limit  $x \rightarrow y$

$$|f'(y)| \leq 0 \Rightarrow f'(y) = 0 \Rightarrow f(y) = c \Rightarrow f(x) = 1$$

$$\int_0^1 1 \cdot dx = 1$$

79.  $\frac{dx}{dt} = 3 \sec^2 t$

$$\frac{dy}{dt} = 3 \sec t \tan t$$

$$\frac{dy}{dx} = \frac{\tan t}{\sec t} = \sin t$$

$$\begin{aligned} \frac{d^2y}{dx^2} &= \cos t \frac{dt}{dx} \\ &= \frac{\cos t}{3 \sec^2 t} = \frac{\cos^3 t}{3} = \frac{1}{3 \cdot 2\sqrt{2}} = \frac{1}{6\sqrt{2}} \end{aligned}$$

80.  $\boxed{a_1} \boxed{a_2} \boxed{a_3}$

Number of numbers =  $5^3 - 1$

$$\boxed{a_4} \boxed{a_1} \boxed{a_2} \boxed{a_3}$$

2 ways for  $a_4$

Numbers of numbers =  $2 \times 5^3$

Required number  $0020 = 5^3 + 2 \times 5^3 - 1$   
 $= 374$

81.  $x^2 + y^2 - 16x - 20y + 164 = r^2$

$A(8, 10), R_1 = r$

$$(x - 4)^2 + (y - 7)^2 = 36$$

$B(4, 7), R_2 = 6$

$$|R_1 - R_2| < AB < R_1 + R_2$$

$$\Rightarrow 1 < r < 11$$

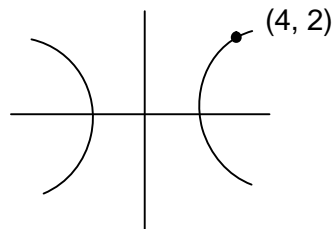
82. Given hyperbola is

$$\frac{x^2}{4} - \frac{y^2}{b^2} = 1$$

Satisfying the point  $(4, 2)$

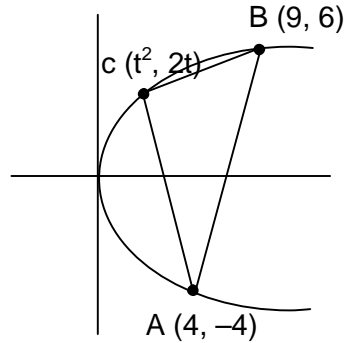
$$\Rightarrow b^2 = \frac{4}{3}$$

$$\Rightarrow e = \frac{2}{\sqrt{3}}$$

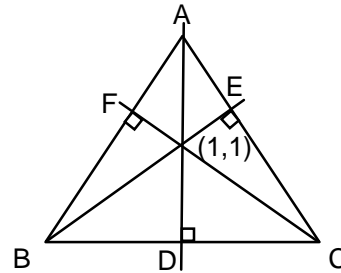


83. For maximum area, tangent at the point c must be parallel to chord BC.

$$\therefore t = \frac{1}{2}$$



84. Equation of AB is  $3x - 2y + 6 = 0$   
 Equation of AC is  $4x + 5y - 20 = 0$ .  
 Equation of BE is  $2x + 3y - 5 = 0$   
 Equation of CF is  $5x - 4y - 1 = 0$   
 $\Rightarrow$  Equation of BC is  
 $26x - 122y = 1675$



85.  $E_1$  : Event of drawing a Red ball and placing a green ball in the bag  
 $E_2$  : Event of drawing a green ball and placing a red ball in the bag

$$E : \text{Event of drawing a red ball in second draw } P(E) = P(E_1) \times P\left(\frac{E}{E_1}\right) + P(E_2) \times P\left(\frac{E}{E_2}\right)$$

$$= \frac{5}{7} \times \frac{4}{7} + \frac{2}{7} \times \frac{6}{7} = \frac{32}{49}$$

86. Line  $x = ay + b, z = cy + d$

$$\Rightarrow \frac{x-b}{a} = \frac{y}{1} = \frac{z-d}{c}$$

$$\text{Line } x = a'z + b', y = c'z + d'$$

$$\Rightarrow \frac{x-b'}{a'} = \frac{y-d'}{c'} = \frac{z}{1}$$

Given both the lines are perpendicular

$$\Rightarrow aa' + c' + c = 0$$

87. Projection of  $\vec{b}$  on  $\vec{a} = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}|} = |\vec{a}|$

$$\Rightarrow b_1 + b_2 = 2 \quad \dots\dots\dots(1)$$

$$\text{and } (\vec{a} + \vec{b}) \perp \vec{c} \Rightarrow (\vec{a} + \vec{b}) \cdot \vec{c} = 0$$

$$\Rightarrow 5b_1 + b_2 = -10 \quad \dots\dots\dots(2)$$

$$\text{from (1) and (2) } \Rightarrow b_1 = -3 \text{ and } b_2 = 5$$

$$\text{then } |\vec{b}| = \sqrt{b_1^2 + b_2^2 + 2} = 6$$

88. D must be perfect square  
 $\Rightarrow 121 - 24\alpha = \lambda^2$   
 $\Rightarrow$  maximum value of  $\alpha$  is 5  
 $\alpha = 1 \Rightarrow \lambda \notin \mathbb{I}$   
 $\alpha = 2 \Rightarrow \lambda \notin \mathbb{I}$   
 $\alpha = 3 \Rightarrow \lambda \in \mathbb{I} \quad \Rightarrow 3 \text{ integral values}$   
 $\alpha = 4 \Rightarrow \lambda \in \mathbb{I}$   
 $\alpha = 5 \Rightarrow \lambda \in \mathbb{I}$

89.  $f(x) = 2\left(1 + \frac{1}{x-1}\right)$   
 $f'(x) = -\frac{2}{(x-1)^2}$   
 $\Rightarrow f$  is one - one but not onto

90.  $\frac{1}{\sqrt{2k}} \int_0^{\pi/3} \frac{\tan \theta}{\sqrt{\sec \theta}} d\theta = \frac{1}{\sqrt{2k}} \int_0^{\pi/3} \frac{\sin \theta}{\sqrt{\cos \theta}} d\theta$   
 $= -\frac{1}{\sqrt{2k}} 2\sqrt{\cos \theta} \Big|_0^{\pi/3} = -\frac{\sqrt{2}}{\sqrt{k}} \left(\frac{1}{\sqrt{2}} - 1\right)$   
 $\Rightarrow k = 2$