

## MATHEMATICS

- A survey shows that 73% of the persons working in an office like coffee, whereas 65% like tea. If  $x$  denotes the percentage of them, who like both coffee and tea, then  $x$  cannot be :  
(a) 36 (b) 63  
(c) 38 (d) 54
- If the function  $f(x) = \begin{cases} k_1(x - \pi)^2 - 1, & x \leq \pi \\ k_2 \cos x, & x > \pi \end{cases}$  is twice differentiable, then the ordered pair  $(k_1, k_2)$  is equal to :  
(a)  $(\frac{1}{2}, -1)$  (b)  $(\frac{1}{2}, 1)$   
(c)  $(1, 0)$  (d)  $(1, 1)$
- If  $3^{2\sin 2\alpha - 1}$ , 14 and  $3^{4 - 2\sin 2\alpha}$  are the first three terms of an A.P. for some  $\alpha$ , then the sixth term of this A.P. is  
(a) 81 (b) 65  
(c) 66 (d) 78
- If  $S$  is the sum of the first 10 terms of the series  $\tan^{-1}(\frac{1}{3}) + \tan^{-1}(\frac{1}{7}) + \tan^{-1}(\frac{1}{13}) + \tan^{-1}(\frac{1}{21}) + \dots$  then  $\tan(S)$  is equal to :  
(a)  $-\frac{6}{5}$  (b)  $\frac{5}{11}$   
(c)  $\frac{5}{6}$  (d)  $\frac{10}{11}$
- If  $2^{10} + 2^9 \cdot 3^1 + 2^8 \cdot 3^2 + \dots + 2 \cdot 3^9 + 3^{10} = 3^{10} = S - 2^{11}$  then  $S$  is equal to  
(a)  $3^{11}$  (b)  $2 \cdot 3^{11}$   
(c)  $\frac{3^{11}}{2} + 2^{10}$  (d)  $3^{11} - 2^{12}$
- If the common tangent to the parabolas,  $y^2 = 4x$  and  $x^2 = 4y$  also touches the circles,  $x^2 + y^2 = c^2$ , then  $c$  is equal to :  
(a)  $\frac{1}{\sqrt{2}}$  (b)  $\frac{1}{2\sqrt{2}}$  (c)  $\frac{1}{2}$  (d)  $\frac{1}{4}$
- If  $y = y(x)$  is the solution of the differential equation  $\frac{5+e^x dy}{2+y dx} + e^x = 0$  satisfying  $y(0) = 1$ , then a value of  $y(\log_e 13)$  is  
(a) -1 (b) 0 (c) 2 (d) 1
- If  $\int (e^{2x} + 2e^x - e^{-x} - 1)e^{(e^x + e^{-x})} dx = g(x)e^{(e^x + e^{-x})} + c$ , where  $c$  is a constant of integration, then  $g(0)$  is equal to :  
(a) 1 (b)  $e$  (c)  $e^2$  (d) 2
- If  $\alpha$  is the positive root of the equation,  $p(x) = x^2 - x - 2 = 0$ , then  $\lim_{x \rightarrow \alpha} \frac{\sqrt{1 - \cos(p(x))}}{x + \alpha - 4}$  is equal to :  
(a)  $\frac{3}{2}$  (b)  $\frac{3}{\sqrt{2}}$   
(c)  $\frac{1}{\sqrt{2}}$  (d)  $\frac{1}{2}$
- If the co-ordinates of two points A and B are  $(\sqrt{7}, 0)$  and  $(-\sqrt{7}, 0)$  respectively and P is any point on the conic,  $9x^2 + 16y^2 = 144$ , then  $PA + PB$  is equal to :  
(a) 8 (b) 16 (c) 9 (d) 6
- The product of the roots of the equation  $9x^2 - 18|x| + 5 = 0$  is :  
(a)  $\frac{25}{81}$  (b)  $\frac{5}{27}$   
(c)  $\frac{25}{9}$  (d)  $\frac{5}{9}$
- If the volume of a parallelepiped, whose conterminous edges are given by the vectors  $\vec{a} = \hat{i} + \hat{j} + n\hat{k}$ ,  $\vec{b} = 2\hat{i} + 4\hat{j} - n\hat{k}$  and  $\vec{c} = \hat{i} + n\hat{j} + 3\hat{k}$  ( $n \geq 0$ ), is 158 cubic units, then :  
(a)  $n = 7$  (b)  $n = 9$   
(c)  $\vec{b} \cdot \vec{c} = 10$  (d)  $\vec{a} \cdot \vec{c} = 17$
- If the point P on the curve,  $4x^2 + 5y^2 = 20$  is farthest from the point Q(0, -4) then  $PQ^2$  is equal to :  
(a) 29 (b) 48  
(c) 21 (d) 36
- If  $(a, b, c)$  is the image of the point  $(1, 2, -3)$  in the line,  $\frac{x+1}{2} - \frac{y-3}{-2} = \frac{z}{-1}$ , then  $a + b + c$  is equal to :  
(a) 3 (b) -1 (c) 2 (d) 1
- If the four complex numbers  $z, \bar{z}, \bar{z} - 2\text{Re}(\bar{z})$  and  $z - 2\text{Re}(z)$  represent the vertices of a square of side 4 units in the Argand plane, then  $|z|$  is equal to :  
(a) 4 (b) 2  
(c)  $4\sqrt{2}$  (d)  $2\sqrt{2}$
- If the minimum and the maximum values of the function  $f: [\frac{\pi}{4}, \frac{\pi}{2}] \rightarrow \mathbb{R}$ , defined by  $f(\theta) = \begin{vmatrix} -\sin^2\theta & -1 - \sin^2\theta & 1 \\ -\cos^2\theta & -1 - \cos^2\theta & 1 \\ 12 & 10 & -2 \end{vmatrix}$  are  $m$  and  $M$  respectively, then the ordered pair  $(m, M)$  is equal to :  
(a)  $(-4, 4)$  (b)  $(0, 2\sqrt{2})$   
(c)  $(-4, 0)$  (d)  $(0, 4)$
- The negation of the Boolean expression  $x \leftrightarrow \sim y$  is equivalent to :  
(a)  $(\sim x \wedge y) \vee (\sim x \wedge \sim y)$  (b)  $(x \wedge y) \vee (\sim x \wedge \sim y)$   
(c)  $(x \wedge \sim y) \vee (\sim x \wedge y)$  (d)  $(x \wedge y) \wedge (\sim x \vee \sim y)$
- Let  $\lambda \in \mathbb{R}$ . The system of linear equations  $2x_1 - 4x_2 + \lambda x_3 = 1$   
 $x_1 - 6x_2 + x_3 = 2$   
 $\lambda x_1 - 10x_2 + 4x_3 = 3$   
is inconsistent for :  
(a) every value of  $\lambda$   
(b) exactly two values of  $\lambda$   
(c) exactly one positive value of  $\lambda$   
(d) exactly, one negative value of  $\lambda$
- The mean and variance of 7 observations are 8 and 16, respectively. If five observations are 2, 4, 10, 12, 14 then the absolute difference of the remaining two observations is  
(a) 1 (b) 2 (c) 3 (d) 4
- The value of  $\int_{-\pi/2}^{\pi/2} \frac{1}{1+e^{\sin x}} dx$  is :  
(a)  $\frac{\pi}{4}$  (b)  $\frac{\pi}{2}$  (c)  $\frac{3\pi}{2}$  (d)  $\pi$
- The number of words, with or without meaning, that can be formed by taking 4 letters at a time from the letters of the word 'SYLLABUS' such that two letters are distinct and two letters are alike, is \_\_\_\_\_

22. The natural number  $m$ , for which the coefficient of  $x$  in the binomial expansion of  $(x^m + \frac{1}{x^2})^{22}$  is 1540, is \_\_\_\_\_
23. If the line,  $2x - y + 3 = 0$  is at a distance  $\frac{1}{\sqrt{5}}$  and  $\frac{2}{\sqrt{5}}$  from the lines  $4x - 2y + \alpha = 0$  and  $6x - 3y + \beta = 0$ , respectively, then the sum of all possible values of  $\alpha$  and  $\beta$  is \_\_\_\_\_
24. Let  $f(x) = x \cdot \left[ \frac{x}{2} \right]$ , for  $-10 < x < 10$ , where  $[t]$  denotes the greatest integer function. Then the number of points of discontinuity of  $f$  is equal to \_\_\_\_\_
25. Four fair dice are thrown independently 27 times. Then the expected number of times at least two dice show up a three or a five, is \_\_\_\_\_

## ANSWER

1. (a) 2. (b) 3. (c) 4. (c) 5. (a) 6. (a) 7. (a) 8. (d) 9. (b) 10. (a)  
11. (a) 12. (c) 13. (d) 14. (c) 15. (d) 16. (c) 17. (b) 18. (d) 19. (b) 20. (b)  
21. (240.00) 22. (13.00) 23. (30.00) 24. (08.00) 25. (11.00)